

A Tutorial Introduction to Power Factor Correction

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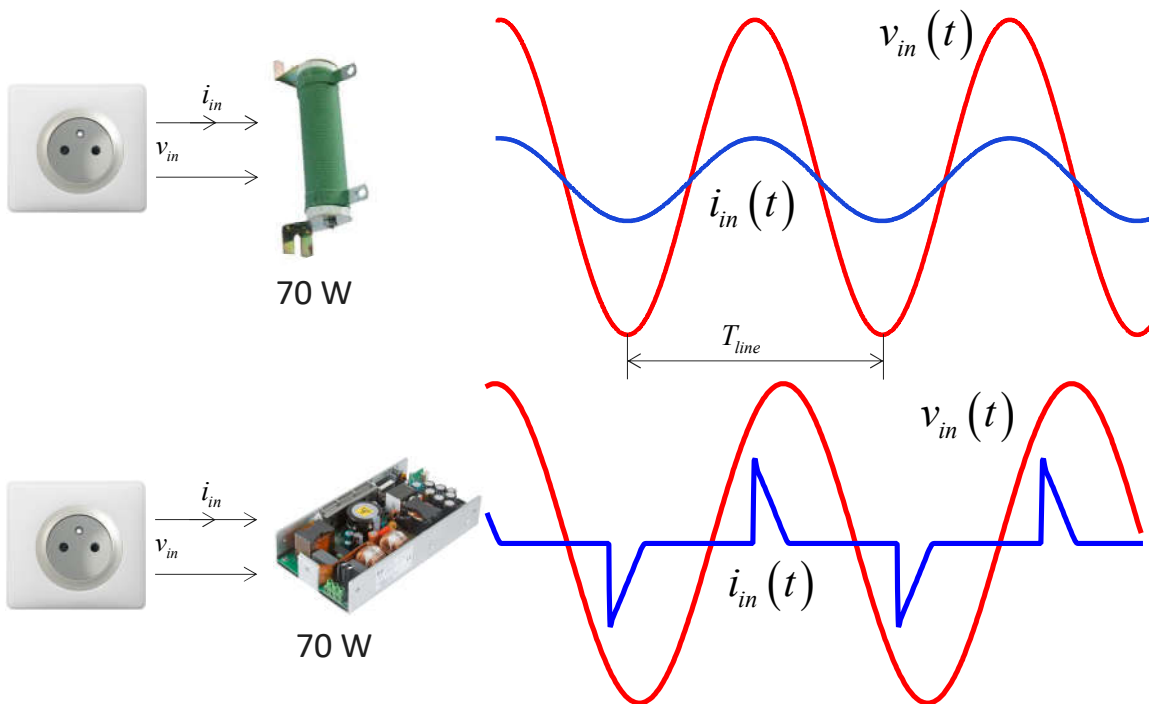
IEEE Senior Member

Agenda

- Notions of Power Factor
- Power Factor Correction Structures
- Processing the Power
- Loop Compensation of a PFC
- Solutions from Future Suppliers

What is Power Factor?

- The goal of any power factor correction circuit is to emulate a resistance
- The absorbed current must be sinusoidal and in phase with the input voltage



$$p_{in}(t) = i_{in}(t)v_{in}(t) = \frac{v_{in}(t)}{R}v_{in}(t)$$

$$P_{in,avg} = \frac{1}{T_{line}} \int_0^{T_{line}} p_{in}(t) \cdot dt = 70 \text{ W}$$

$$P_{in,app} = V_{in,rms} \cdot I_{in,rms} = 85 \times 823m = 70 \text{ VA}$$

$$PF = \frac{\text{active power}}{\text{apparent power}} = \frac{[\text{W}]}{[\text{V} \cdot \text{A}]} = 1$$

$$P_{in,avg} = \frac{1}{T_{line}} \int_0^{T_{line}} p_{in}(t) \cdot dt = 70 \text{ W}$$

$$P_{in,app} = V_{in,rms} \cdot I_{in,rms} = 85 \times 1.46 = 124 \text{ VA}$$

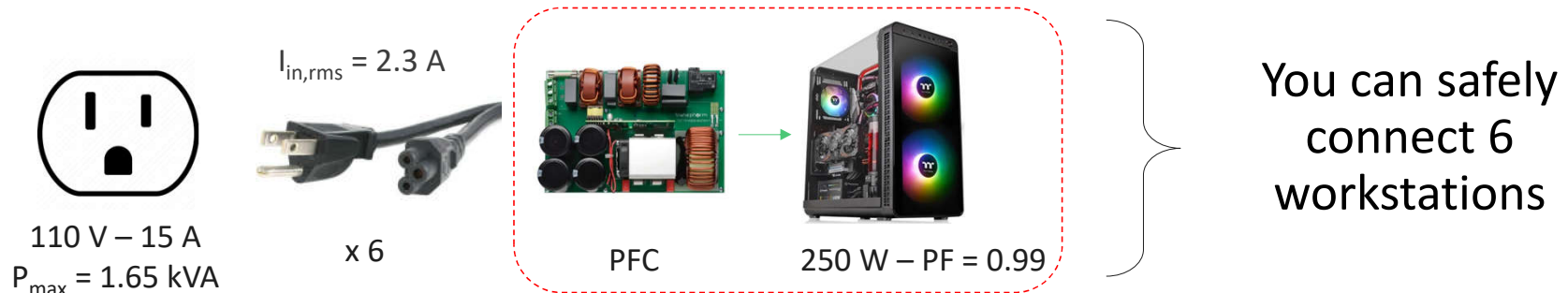
$$PF = \frac{\text{active power}}{\text{apparent power}} = \frac{[\text{W}]}{[\text{V} \cdot \text{A}]} = 0.56$$

What is the Impact of a Low PF?

- Assume a 250-W load absorbed by an equipment from a 110-V 15-A ac outlet
- With a PF of 0.56, the current is $250/110/0.56 \approx 4$ A rms
- ✓ You can safely connect a maximum of 3 devices ($15/4 = 3.75$)

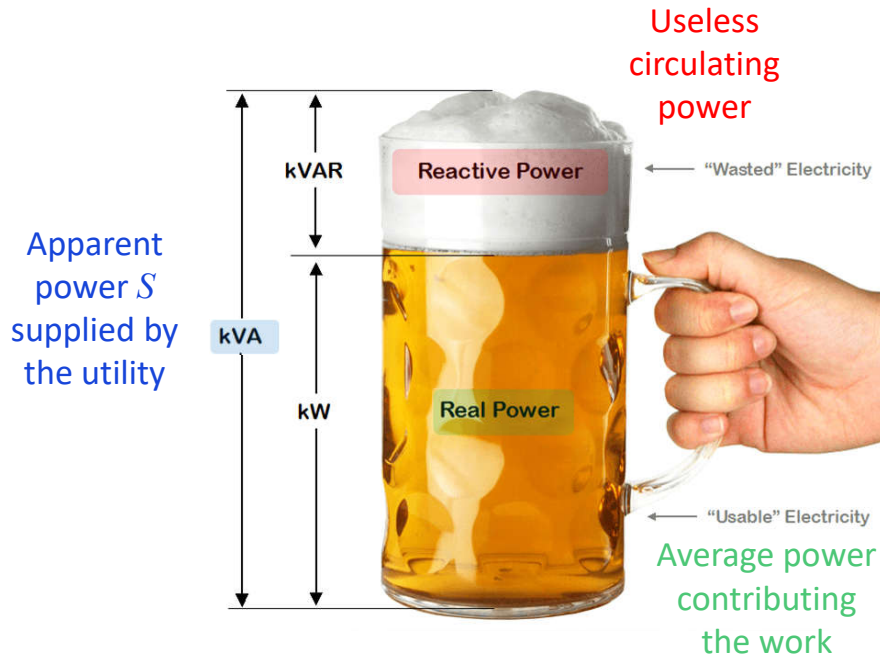


- Add a front-end power factor correction stage to bring PF close to unity



Explaining Power Factor with Beer

- A low power factor will force the circulation of a higher rms current
- Electric wires can overheat and utility companies push for power factor correction
- ✓ A glass of beer with an excessive foam can help appreciate the issue



Over 15kW

Rates 3.0A - 3.1A y 6.x

Billed solely when reactive power exceeds 33% of the active power. It is not applied in the off-peak period (P3 of rate 3.X and P6 of rate 6.X).

$$S [VA] = P [W] + jQ [VAR]$$

$$\left| \frac{P}{PF} \right| = \sqrt{P^2 + Q^2}$$

$$Q = P \sqrt{\frac{1}{PF^2} - 1}$$



If PF < 0.95

$Q [VAR] > 33\% \cdot P [W]$

Power Factor and Distortion

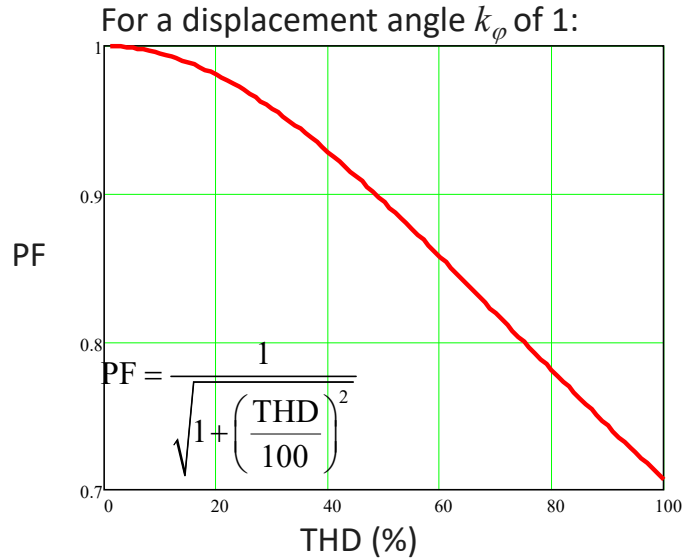
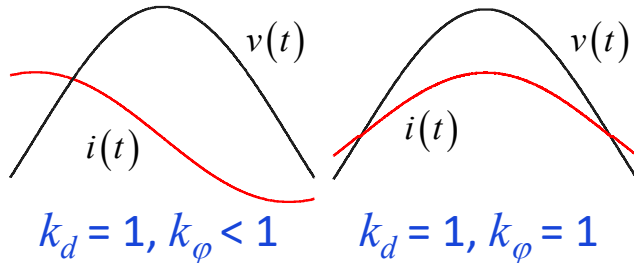
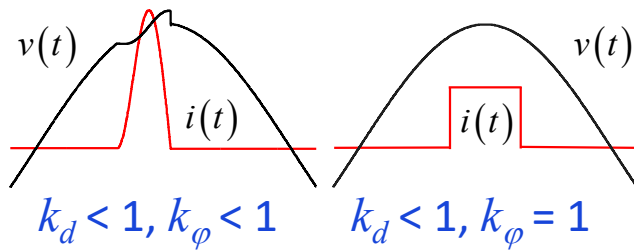
- Power factor depends on two parameters:

$$PF = \frac{I_{1,rms}}{I_{rms}} \cos \varphi = k_d k_\varphi$$

↑ Fundamental rms current
↑ Total rms current

✓ k_d represents the distortion factor

✓ k_φ designates the displacement angle



THD = 30%, PF = 0.958

THD = 10% PF = 0.995

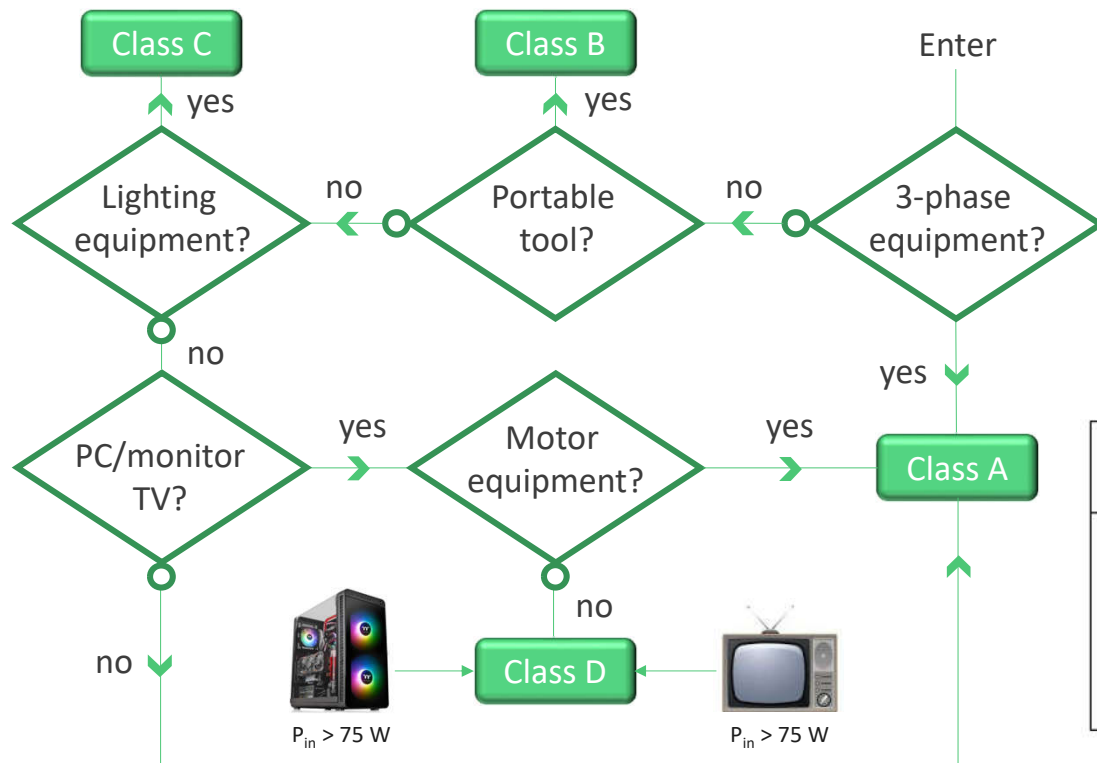
THD = 5% PF = 0.999



Check harmonics limits according to IEC1000-3-2

Equipment Compliance

- The standard EN61000-3-2 defines the class of equipment and associated limits



NORME INTERNATIONALE
INTERNATIONAL STANDARD

CEI IEC
61000-3-2

Deuxième édition
Second edition
2000-08

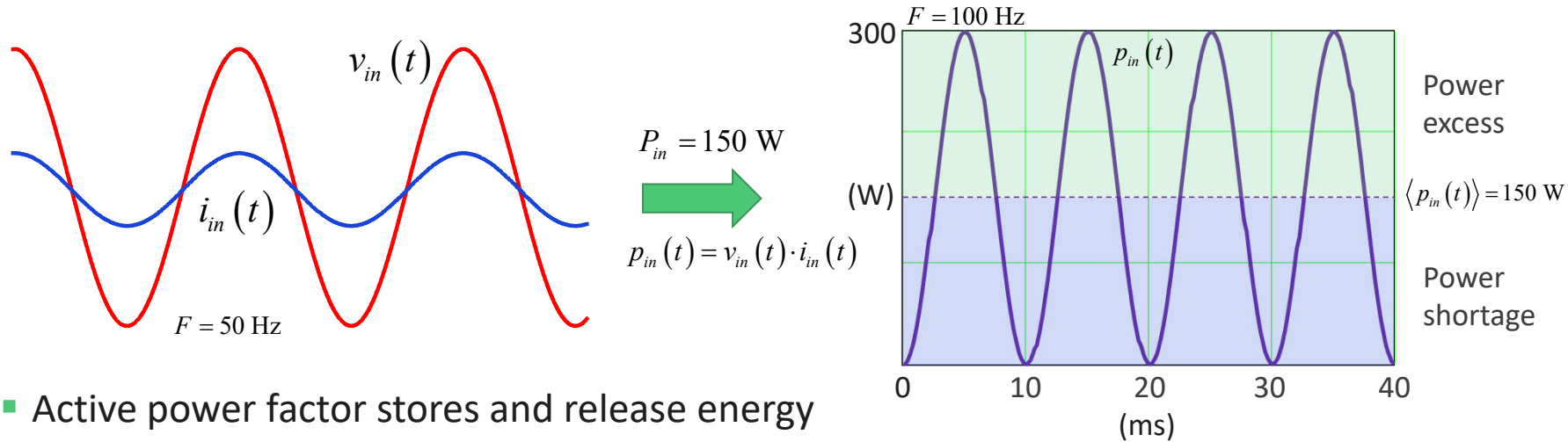


Class D limits

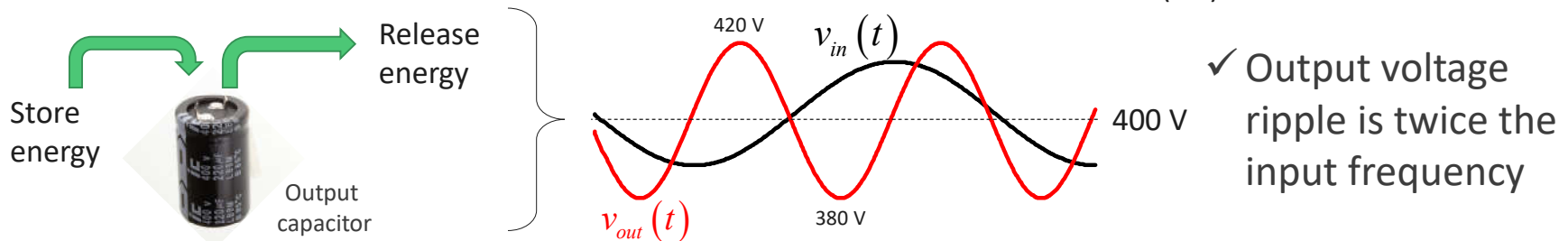
Rang harmonique	Courant harmonique maximal autorisé par watt mA/W	Courant harmonique maximal autorisé A
n		A
3	3,4	2,30
5	1,9	1,14
7	1,0	0,77
9	0,5	0,40
11	0,35	0,33
13 ≤ n ≤ 39 (harmoniques impairs seulement)	$\frac{3,85}{n}$	Voir tableau 1

The Need for Storage

- The goal of a PFC front-end converter is to emulate a resistive load
- The power of a single-phase ac source feeding a resistance involves a squared sinewave



- Active power factor stores and release energy

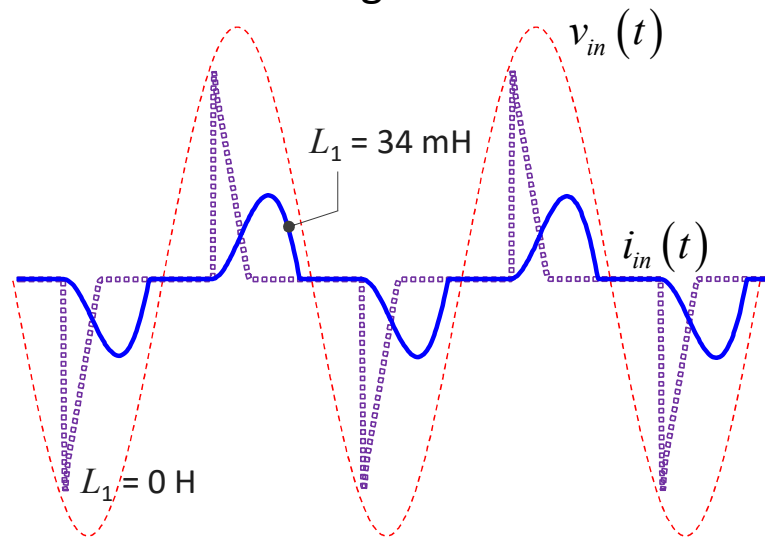
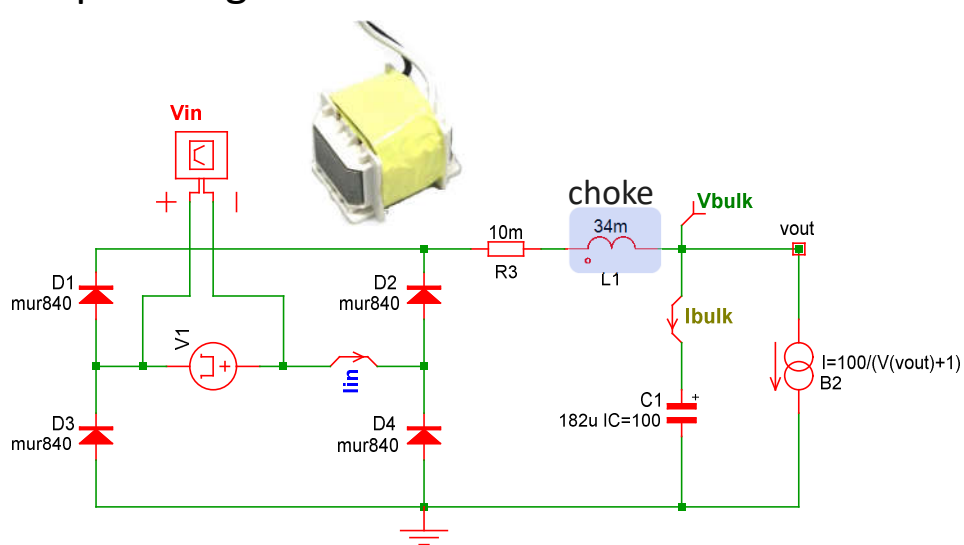


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Passive Power Factor Correction

- Capacitor refueling in a full-bridge rectifier is confined at the sinewave peak
- A very narrow spike is generated, rich of numerous harmonics
- ✓ Spreading the current across the sinewave smooths the current signature



- ❖ Choke is bulky, heavy and induces mechanical stress
- ❖ Reduces rms current but marginal results harmonic-wise



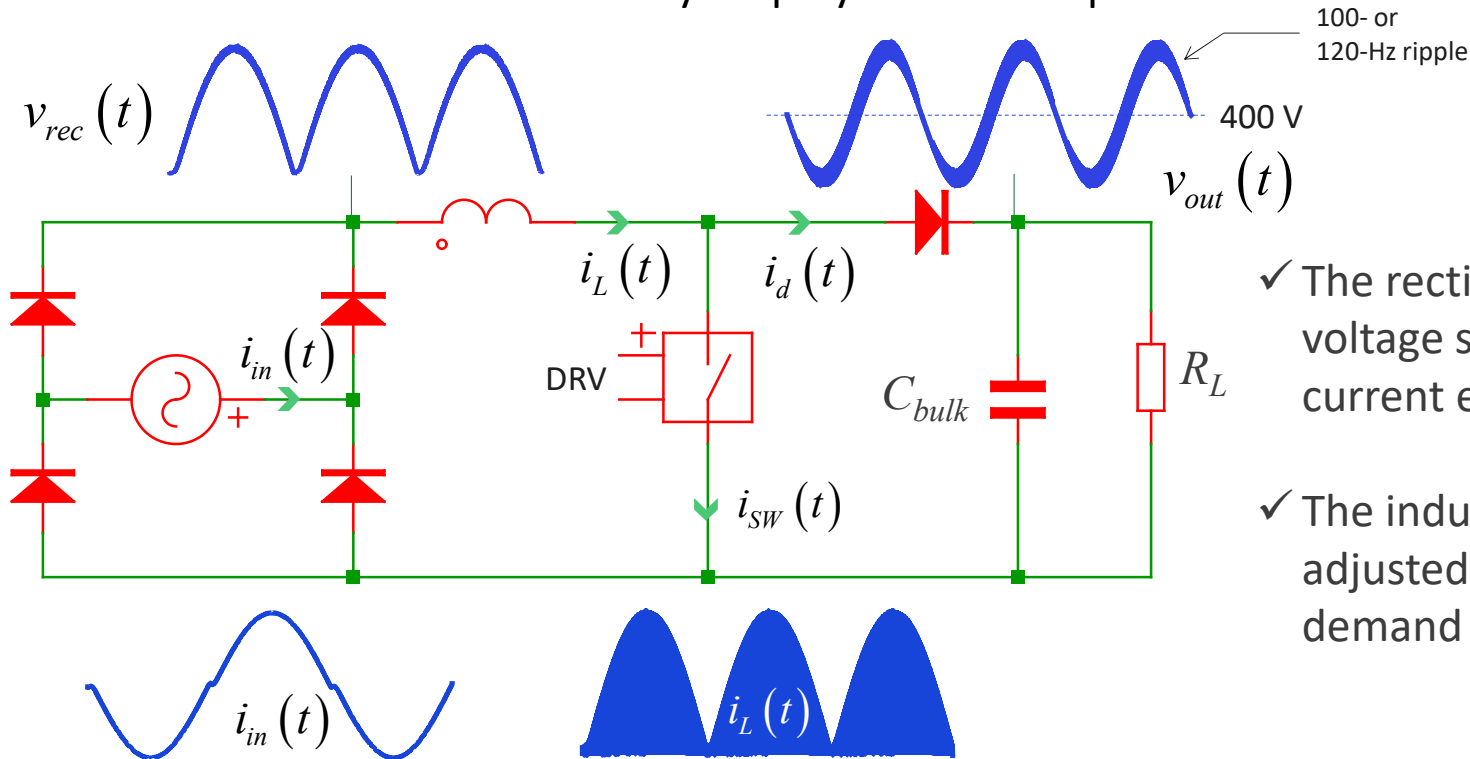
$$P_{out} = 100 \text{ W}$$

$$I_{in,rms} = 1.8 \text{ A without } L$$

$$I_{in,rms} = 1.2 \text{ A with } L = 34 \text{ mH}$$

Active Power Factor Correction

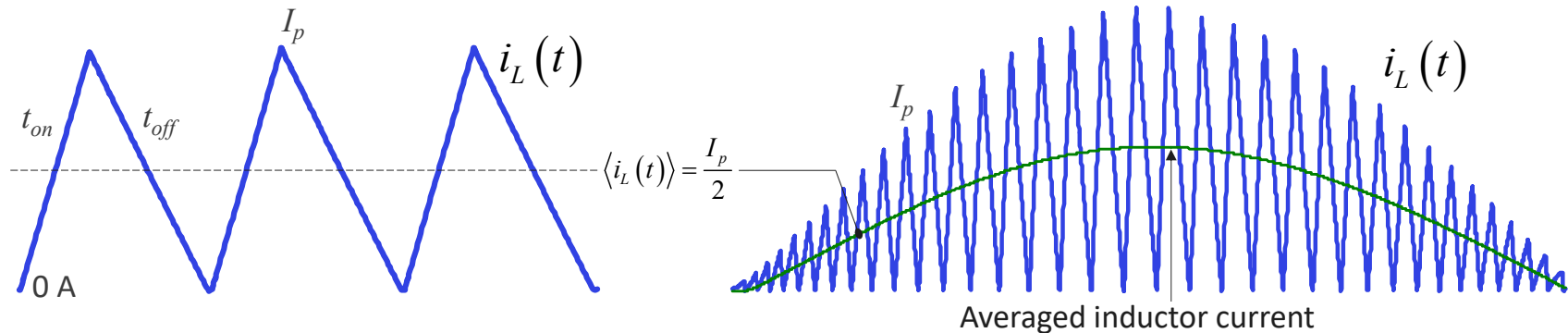
- An active PFC forces a sinusoidal current absorption in phase with the voltage
- A boost converter is traditionally employed for this operation



- ✓ The rectified input voltage sets the inductor current envelope
- ✓ The inductor current is adjusted to match power demand

Conduction Mode – BCM or CrM

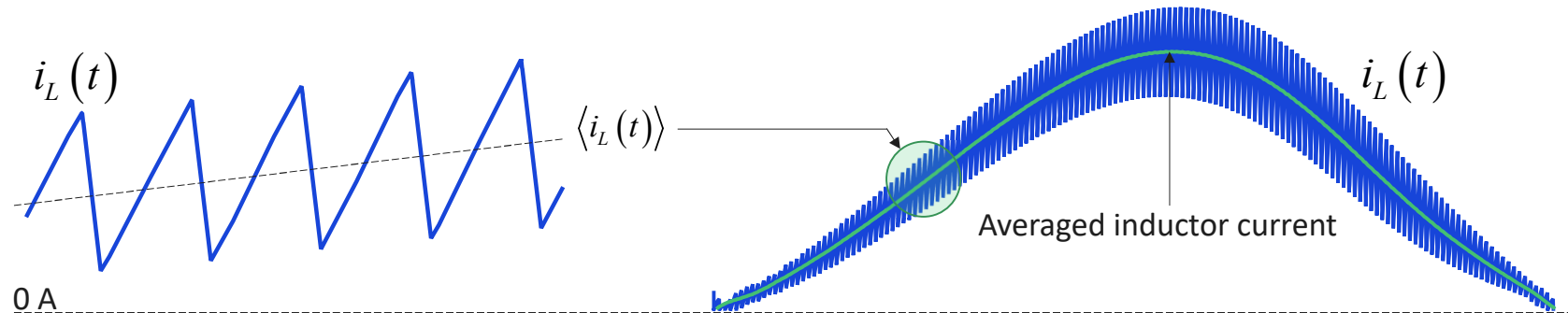
- Inductor current reduces to 0 A before a new cycle starts in **borderline conduction mode**
- ✓ Well suited for power levels up to 300 W or higher with interleaved version
- ✓ Near-zero-voltage switching in some conditions
- ✓ Discontinuous operation reduces t_{rr} -related power dissipation on the diode



- ❖ Variable-frequency switching makes light-load operation less efficient
- ❖ Internal frequency clamp or foldback is generally implemented to reduce losses
- ❖ Large circulating currents inducing conduction (rms) and core losses (ΔI_L)

Conduction Mode - CCM

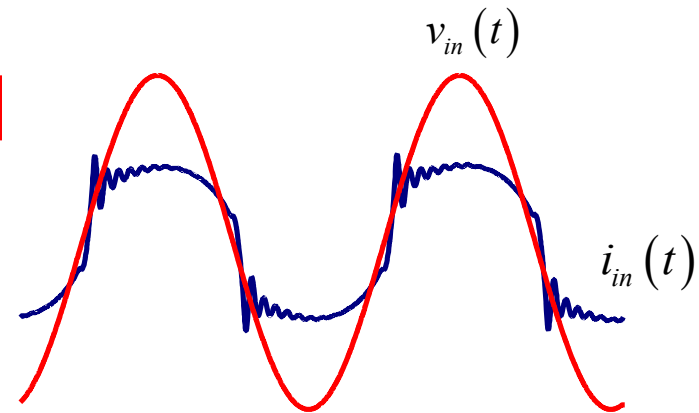
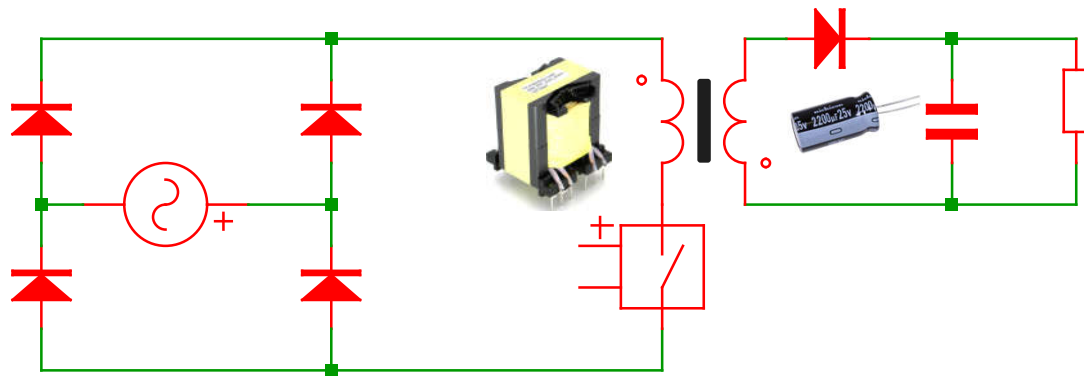
- The inductor current never touches zero within a switching cycle
- ✓ Continuous conduction mode is well suited for high-power converters > 300 W
- ✓ Current can be monitored by an independent loop for best distortion figures
- ✓ Circulating rms currents are minimized with a moderately-low ripple current



- ❖ CCM induces switching losses and low- t_{rr} diodes or SiC types are mandatory
- ❖ Larger inductance value compared to BCM operation
- ❖ Two loops to stabilize in the classical multiplier-based approach

Single-Stage Converters

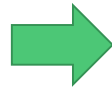
- It is possible to combine a PFC stage with an isolated flyback converter
- This single-stage approach is well adapted to power levels up to 100-150 W
- ✓ The components count is reduced
- ✓ It provides galvanic isolation to the downstream load



- ❖ Large output capacitance for the storing process
- ❖ Fairly-distorted input current barely passes PF specifications
- ❖ Slow-loop operation makes it well suited for lighting systems

Bridgeless PFC

- The bridge hampers overall efficiency with two permanently-conducting diodes



$$P_d \approx 2V_f I_{d,avg}$$

$$I_{F,avg} = \frac{2 \sqrt{2} P_{out}}{\pi V_{ac,LL} \eta}$$

$$P = 300 \text{ W}$$

$$\eta = 100\%$$

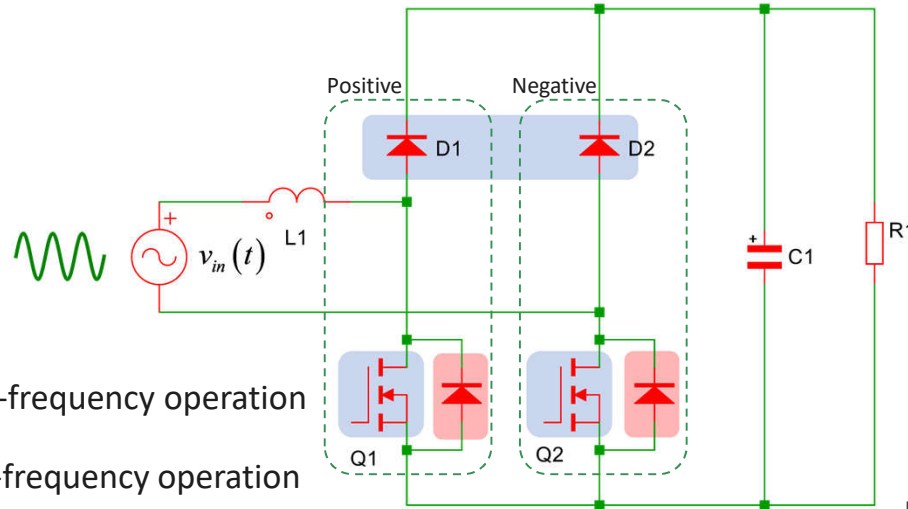
$$V_{ac,LL} = 90 \text{ V rms}$$



$$P_d \approx 5 \text{ W}$$

$$\text{Eff. loss} \approx 1.7\%$$

- The bridgeless PFC ensures one diode conduction via the MOSFET body

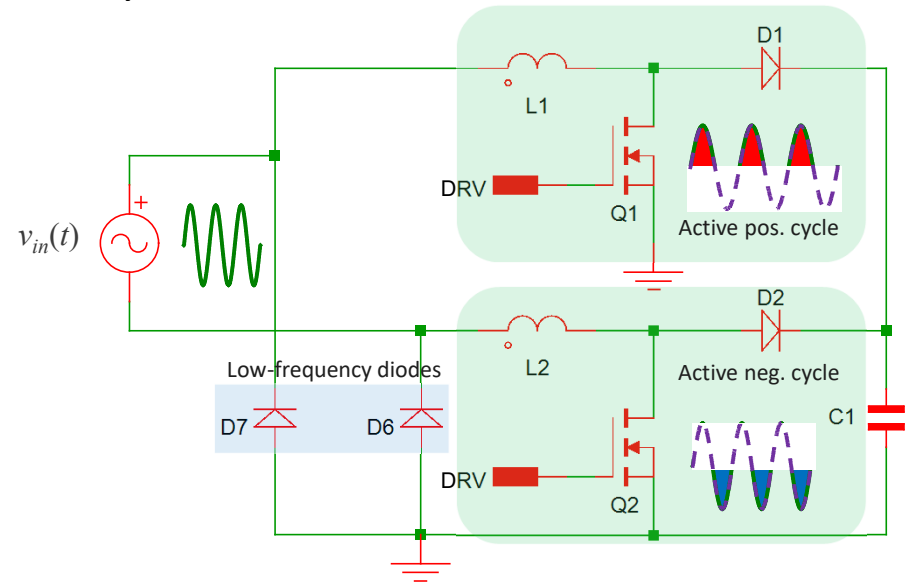
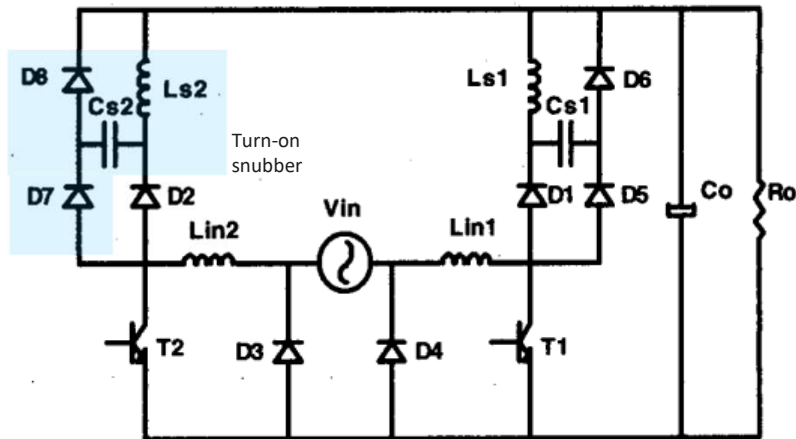


- High-frequency operation
- Low-frequency operation

- ✓ Only one diode is conducting in low frequency
- ✓ The MOSFETs share a common drive signal without caring about line polarity
- ❖ Poor common-mode noise signature

Variation of the Bridgeless PFC

- The original scheme suffers from a poor common-mode EMI signature
- A variation around this circuit was proposed by Ivo Barbi in 1999



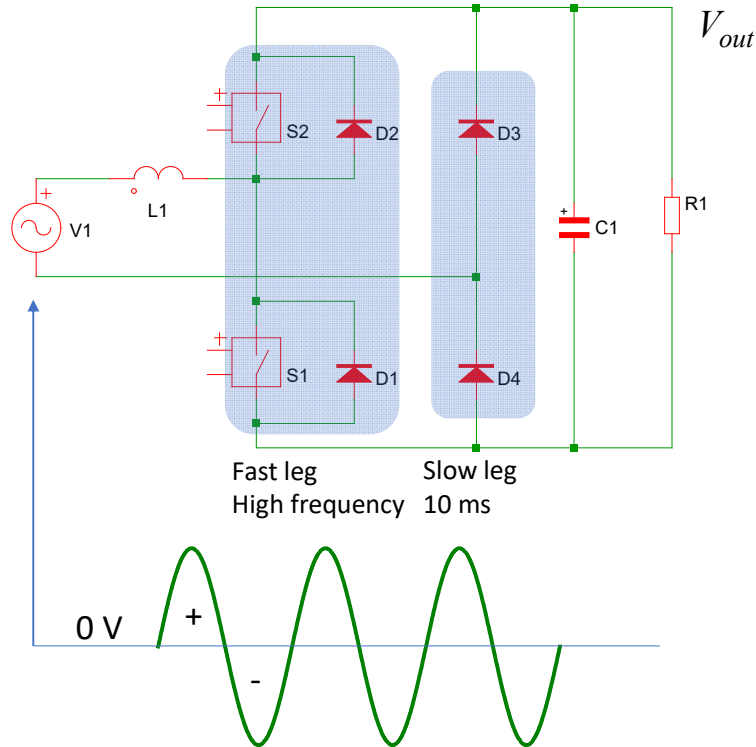
- ✓ Two PFC in parallel driven by the same pattern – easy to drive with one controller
- ✓ Conventional structure automatically activated depending on the line polarity

A. F. de Souza and I. Barbi, *High power factor rectifier with reduced conduction and commutation losses*, 21st International Telecommunications Energy Conference. INTELEC '99 (Cat. No. 99CH37007), 1999

B. J. Turchi, *A High-Efficiency 300-W Bridgeless PFC Stage*, AND8481/D, onsemi, 2014

The Totem-Pole PFC

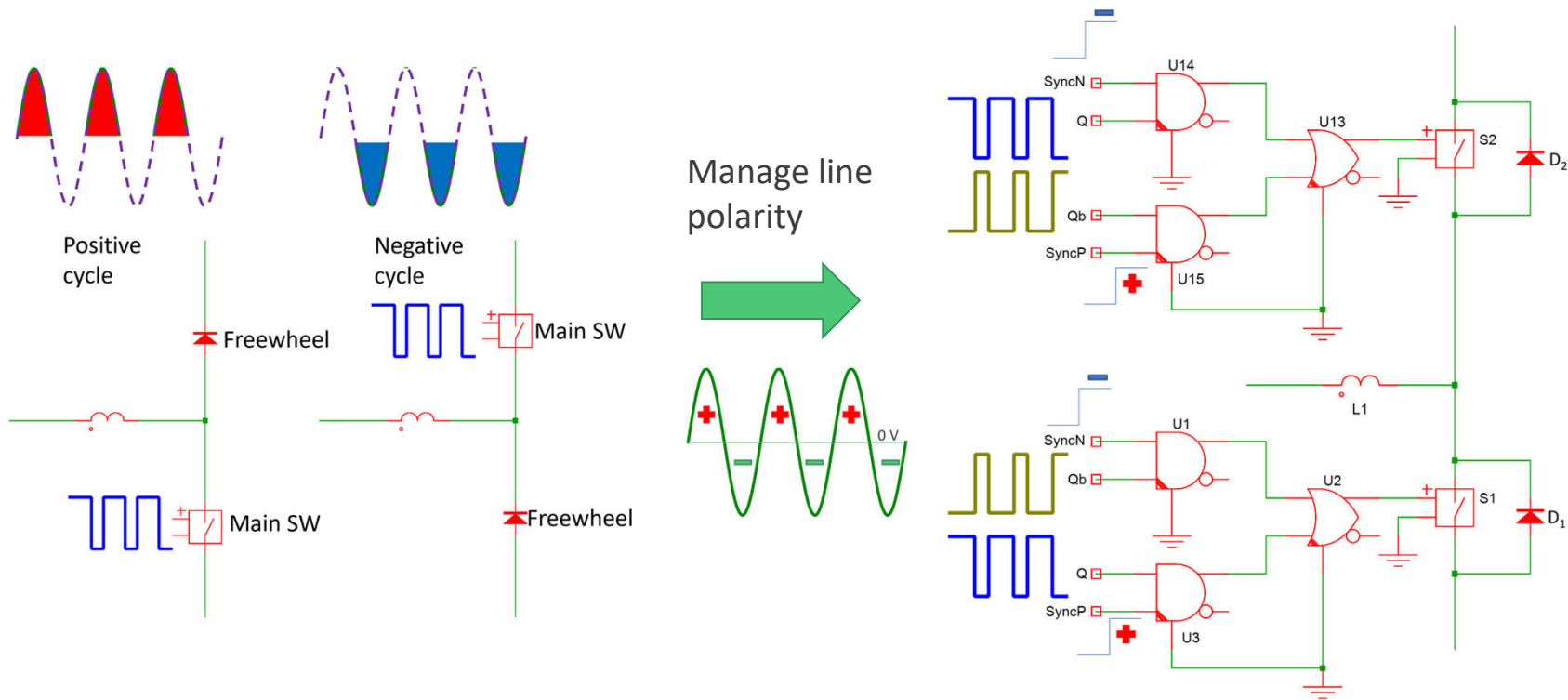
- The two high-frequency switches are connected in a half-bridge configuration
- Two diodes in the slow leg route the low-frequency portion of the input current



- ✓ The fast-leg transistors alternatively perform as power switch and catch diode
- ✓ D_2 and D_1 must be fast diodes with no recovery loss: SiC or GaN transistors are perfect for this function
- ✓ D_3 and D_4 can be controlled-switches for improved efficiency
- ✓ Common-mode noise improved compared to bridgeless PFC

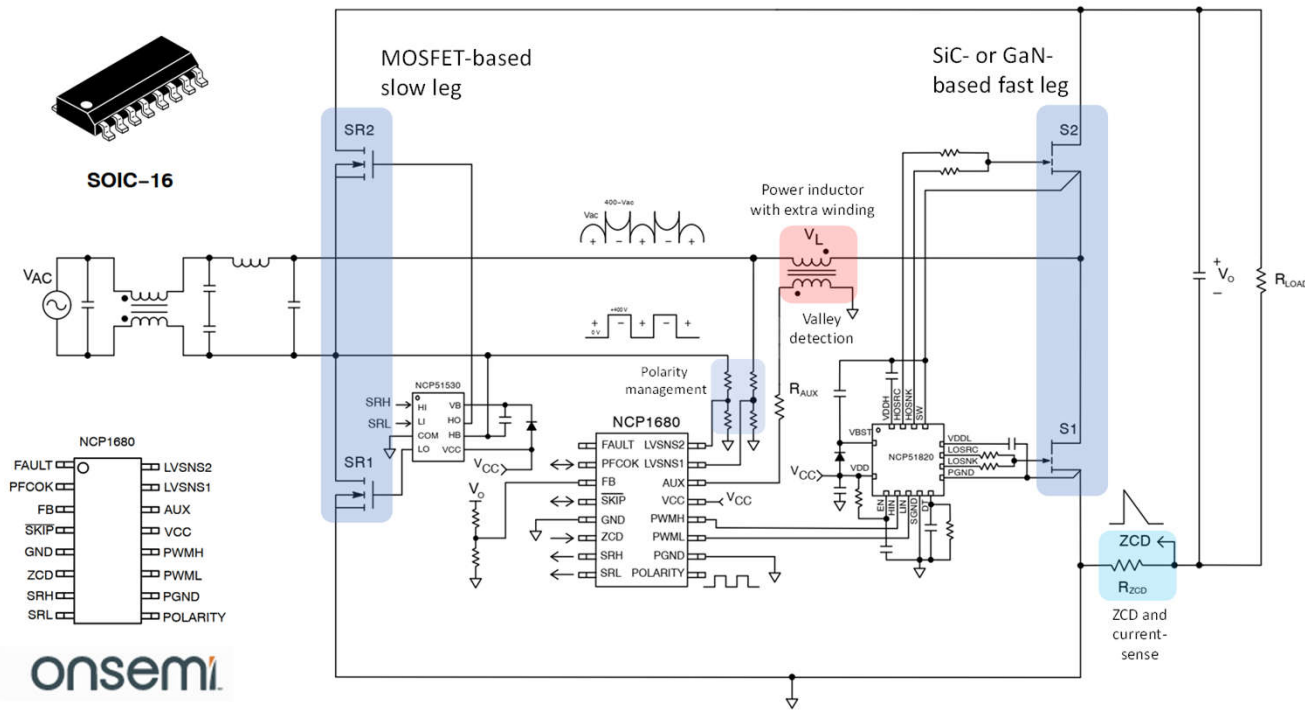
The Need to Detect the Input Line Polarity

- Each fast-leg transistor alternatively plays the role of the switch and the diode
- ✓ The switching element needs instruction on the input line polarity



Dedicated Controllers for TPPFC

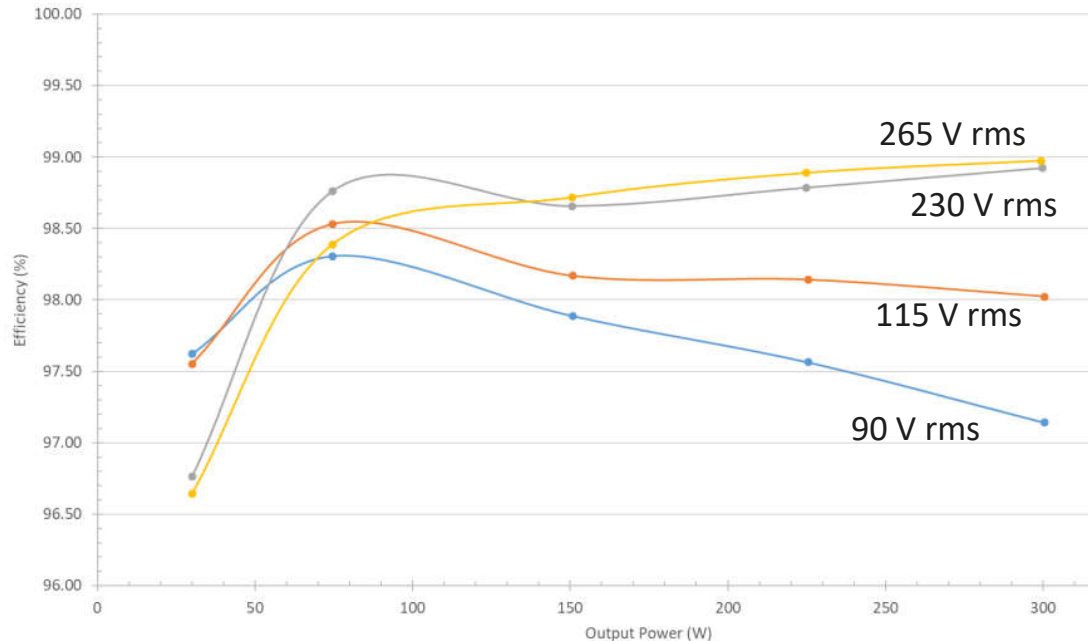
- *onsemi* has introduced two low-voltage controllers operating in BCM and CCM
- ✓ NCP1680 can implement a pre-converter up to 300 W



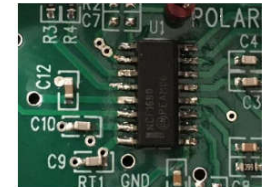
- ✓ One single inductor with auxiliary winding ensures ZVS operation
- ✓ Line management with a pair of resistive dividers
- ✓ Two external drivers dedicated to fast and slow legs: NCP51820 and NCP51530

Efficiency Performance of the BCM TPPFC

- The TPPFC efficiency is excellent compared with a classical approach
- A gain of 1.8% is brought by the all-synchronous approach at 90-V rms input voltage



300-W PFC demonstration board

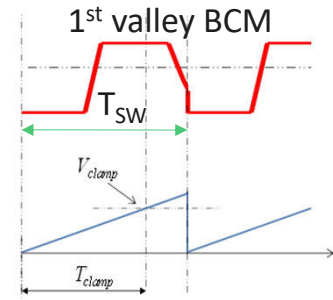
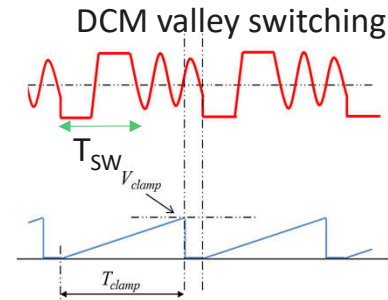
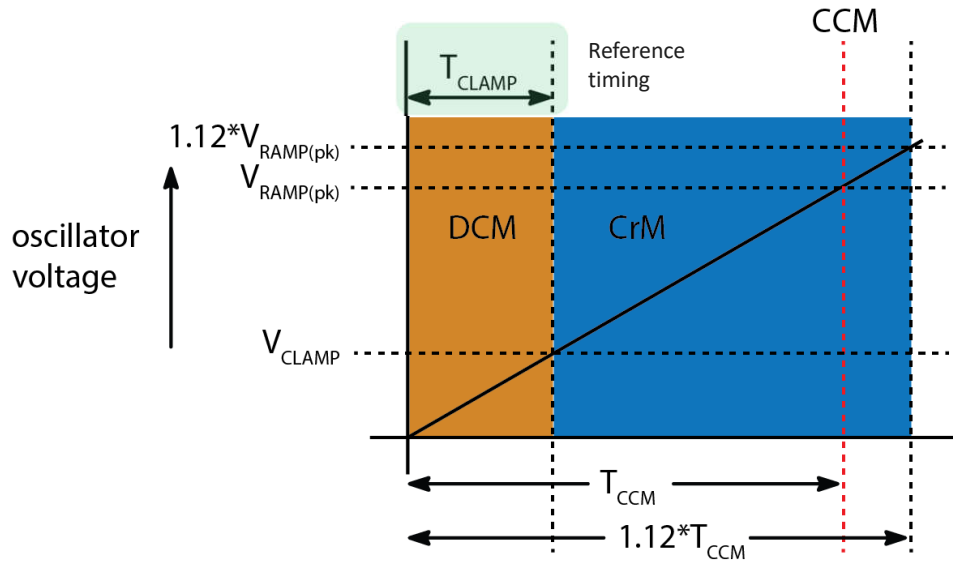


NCP1680

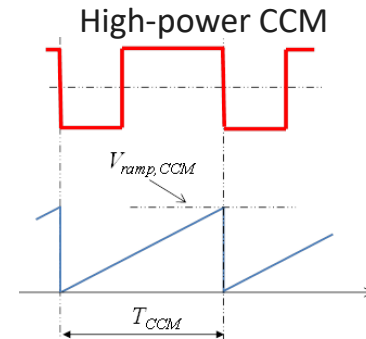
✓ Efficiency approaches 99% at 230 V rms and full power

Multi-Mode Operations

- The downstream converter may operate with different load profiles, low to high current
- CCM is optimized for high power but BCM and DCM bring better efficiency at lighter loads
- ✓ NCP1681 embarks a multi-mode engine smoothly transitioning across all these modes

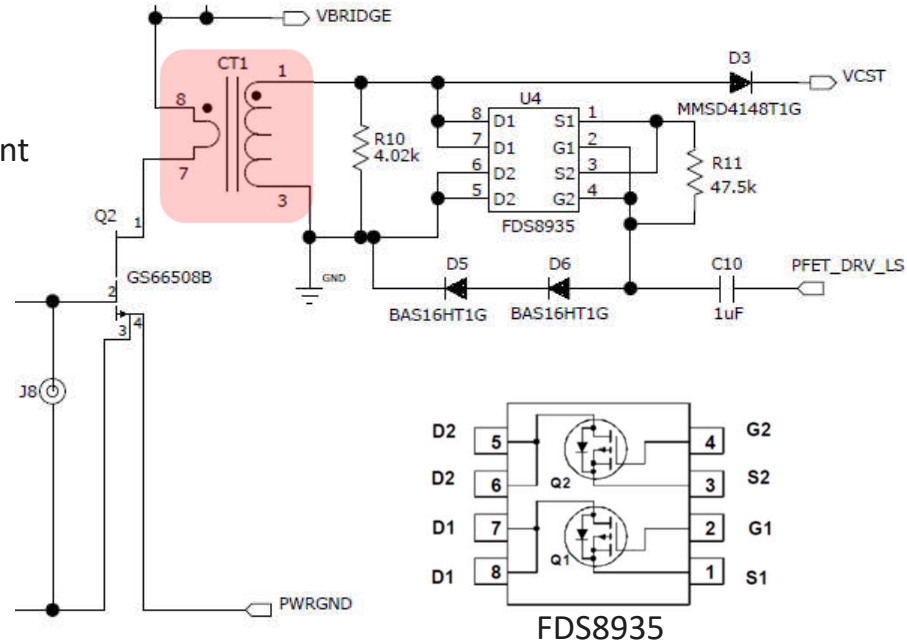
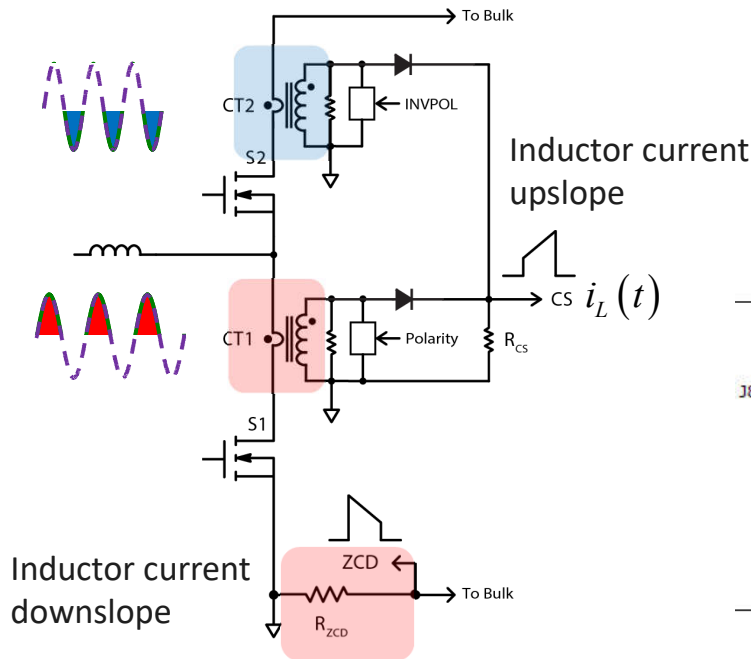


- ✓ The part internally compares operating timings with thresholds to determine the mode
- ✓ The mode is kept during an entire half cycle



Managing Current Transformers

- Fast-leg switches play the main power switch or the rectifier role in a TPPFC
- Current flow in the leg depends on the input line polarity and needs specific action
- ✓ Current transformers secondaries are alternatively shorted depending on line polarity



A Reliable Controller with Fault Management

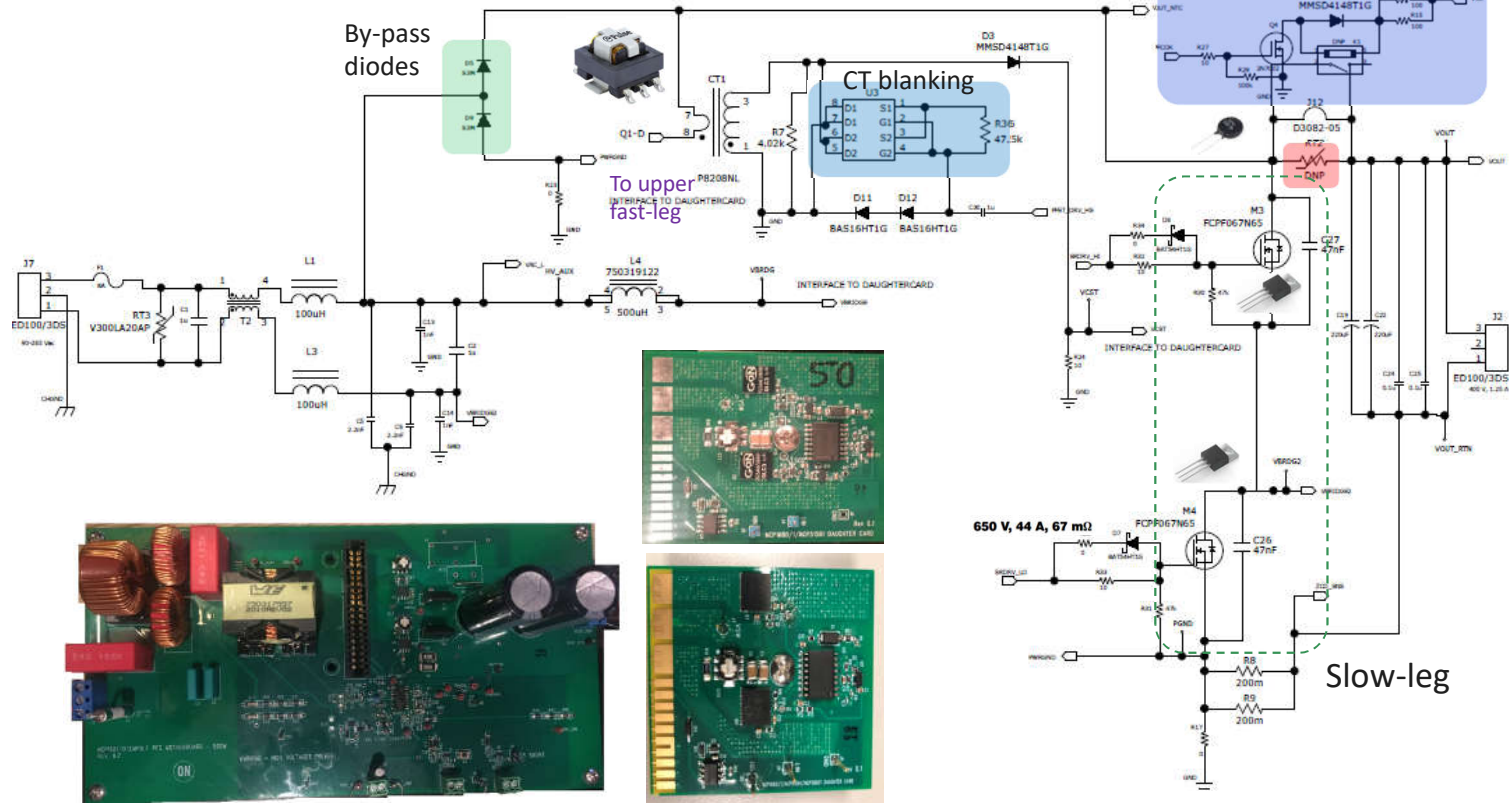
- The controller permanently monitors operating variables for maximum protection
- Some minor faults involve a quick recovery while heavier issues start a 500-ms timer

Fault	Trigger	Cleared By*	Comments / Notes
UVP	$V_{FB} < V_{UVP}$	$V_{FB} > V_{UVP} + V_{UVP(HYS)}$	<ul style="list-style-type: none"> • All DRV pulses are stopped • PFCOK signal pulled to GND • Polarity signal remains ON
Bulk Under-Voltage (BUV)	$V_{FB} < V_{BUV} + PFC_OK$	T_{BUV} expires	<ul style="list-style-type: none"> • BUV stops DRVs (Soft-stop option) • PFCOK signal pulled to GND. • Polarity signal remains on • 500 <u>ms</u> restart timer
Soft OVP	$V_{FB} > V_{softOVP}$	$V_{FB} < V_{OVPrecover}$	<ul style="list-style-type: none"> • Fast leg DRVs disabled if soft OVP sequence completes • All other signals remain active • Soft start on recovery
Hard OVP	$V_{FB} > V_{hardOVP}$	$V_{FB} < V_{OVPrecover}$	<ul style="list-style-type: none"> • Fast DRV pulses are stopped immediately • Polarity remains on • Slow leg and open loop drive signals remain ON • Soft start on recovery

- ✓ UVP or under-voltage protection monitors the FB pin and checks for a bias before delivering pulses
- ✓ BUV or bulk under-voltage checks that the output voltage is above 80% of its nominal value
- ✓ Soft OVP is active when a benign overshoot is detected like a load release
- ✓ Hard OVP can be seen as more severe fault in case of stronger overshoot or loop failure

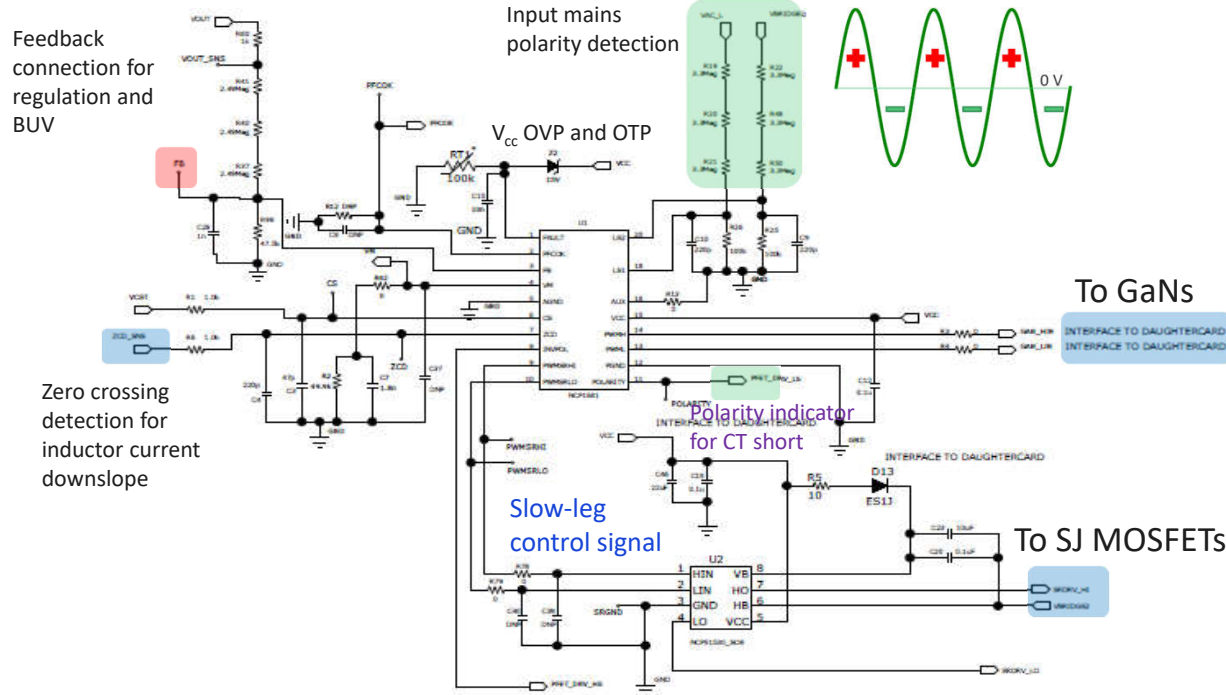
NCP1681 Evaluation Board

- A 500-W demonstration board operated in multi-mode

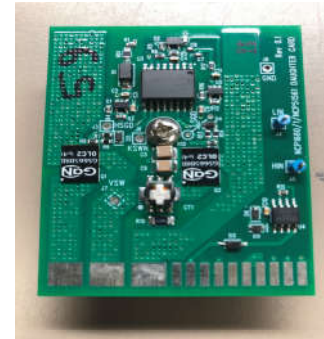


The Control Section

- The NCP1681 senses the polarity via two resistive networks
- The slow-leg requires a bootstrapped driver but of lesser speed than for GaNs



✓ One option with isolated gate driver NCP51561 and discrete GaNs (GS66508B)

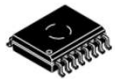
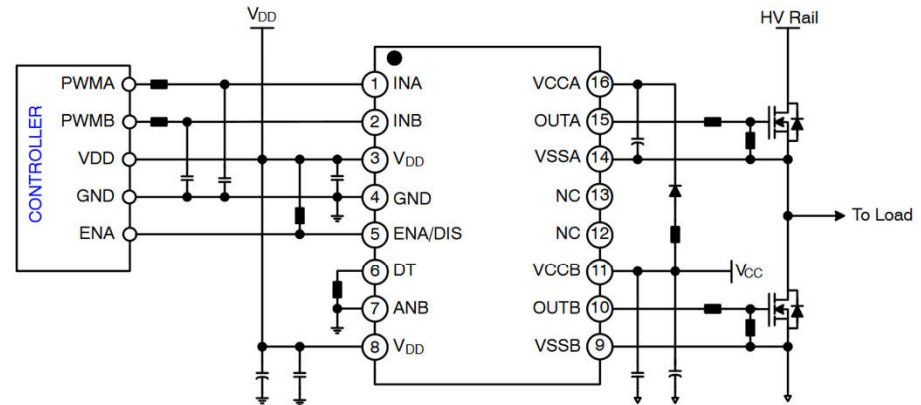
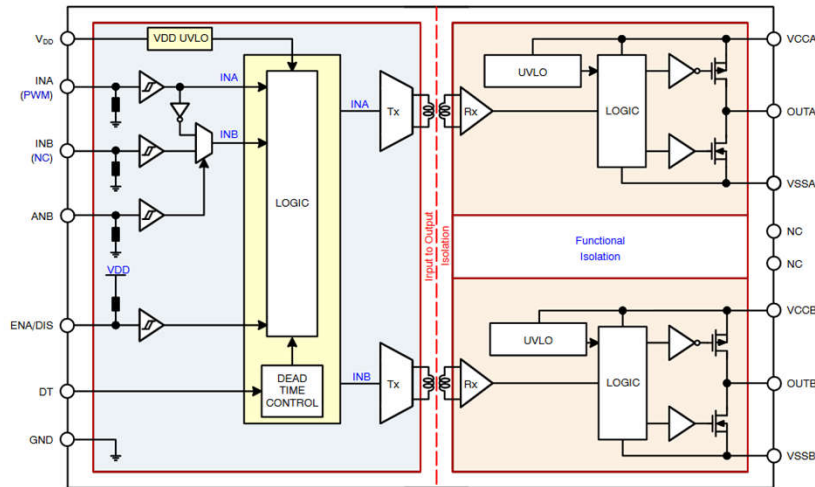


✓ One option with one NCP51561 and two NCP58921



NCP51561 Half-Bridge Driver

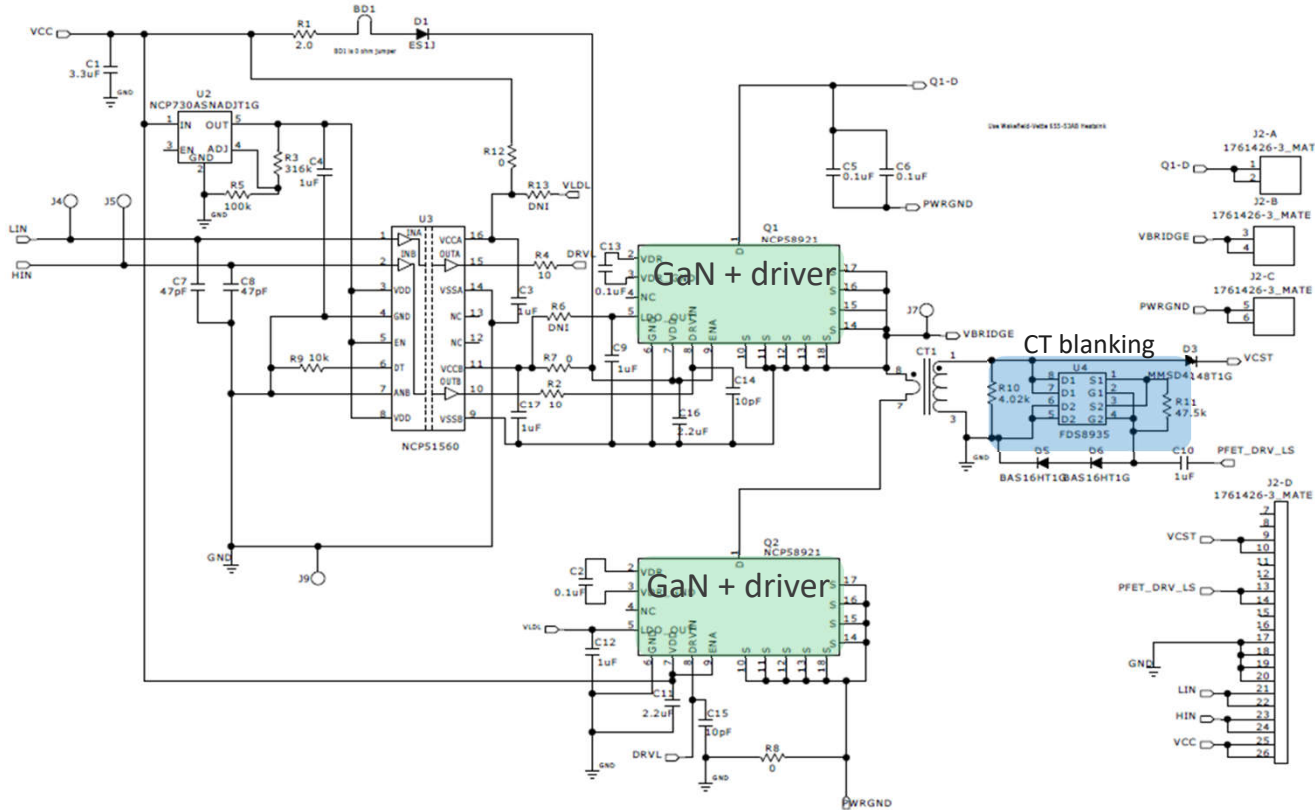
- Isolated drivers are preferred for the fast leg considering switching speed and noise
- ✓ Differential voltage up to 1.5 kV between channels
- ✓ 5-ns delay matching and pulse distortion
- ✓ Common Mode Transient Immunity greater than 200 V/ns



SOIC-16 WB

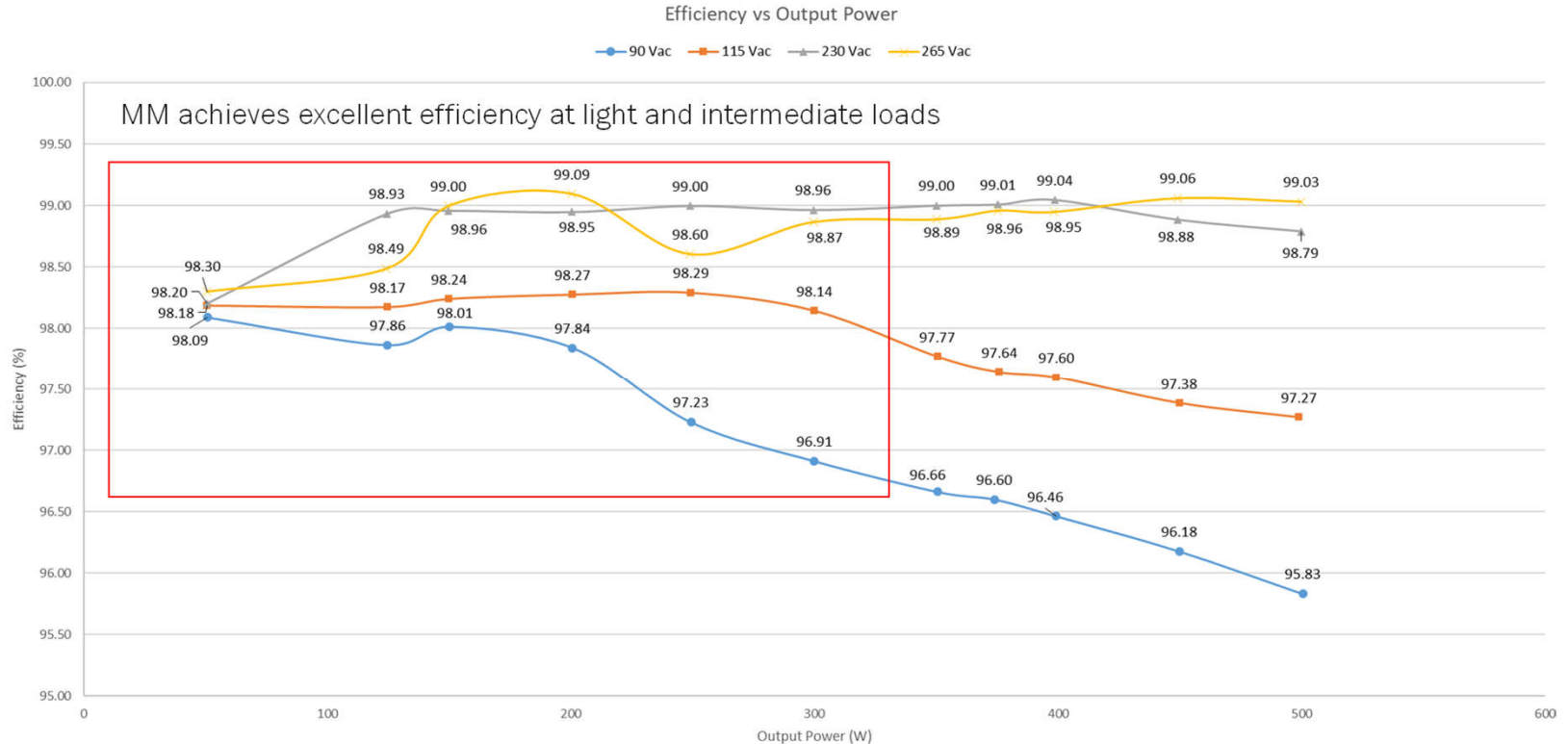
NCP58921 Integrated GaN Driver

- Integrated GaN and driver simplifies PCB layout and reduces BOM cost



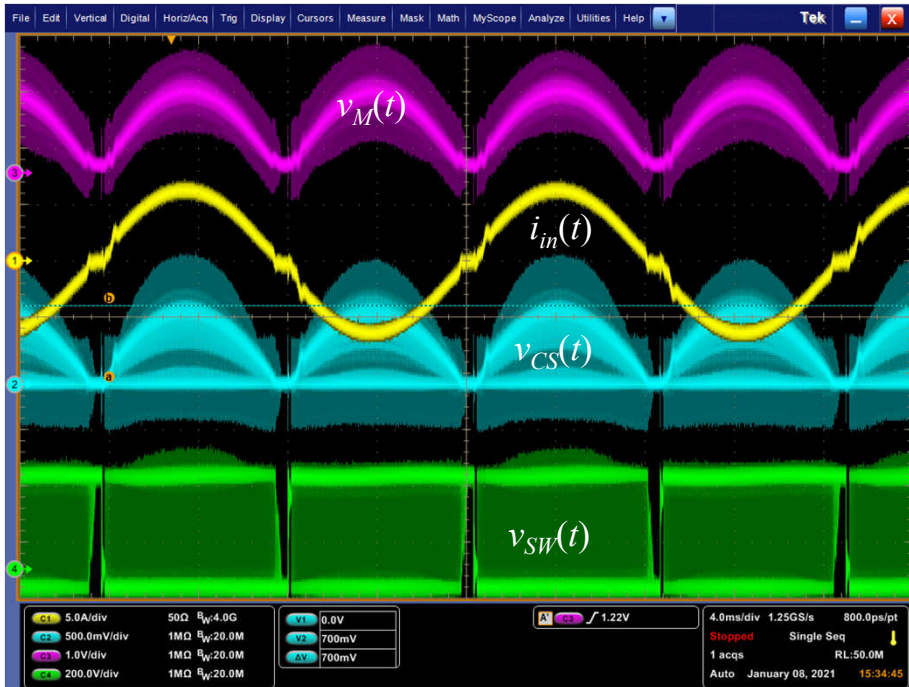
Efficiency Charts with Multi-Mode Engine

- The multi-mode engines clearly shows its positive effects in light-load conditions

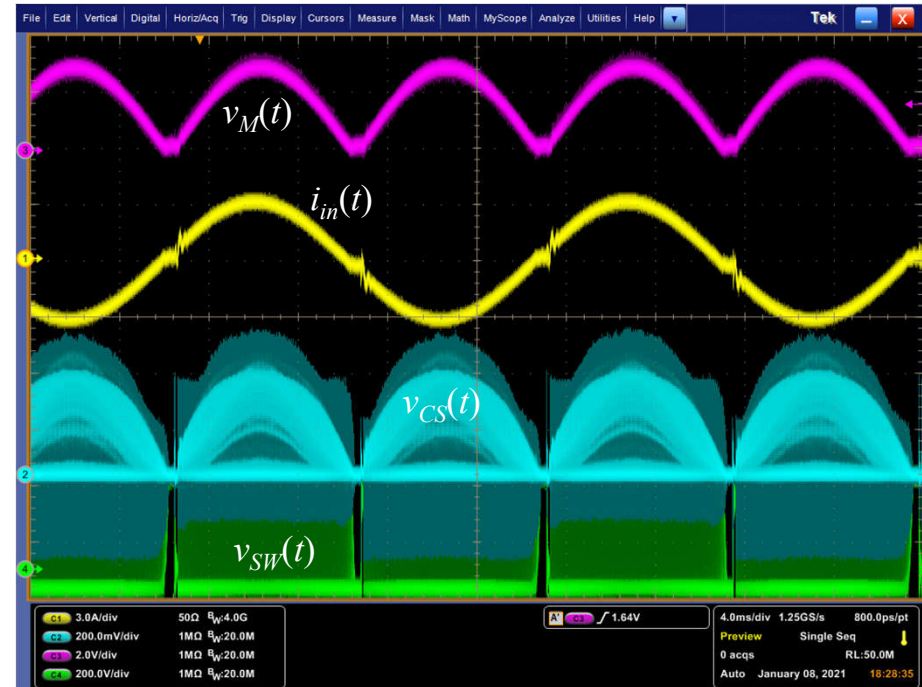


Operating Waveforms

- The part excels in distortion performance which keeps below 5% at full load



$V_{in} = 115 \text{ V rms} - \text{THD} = 4.2\%$



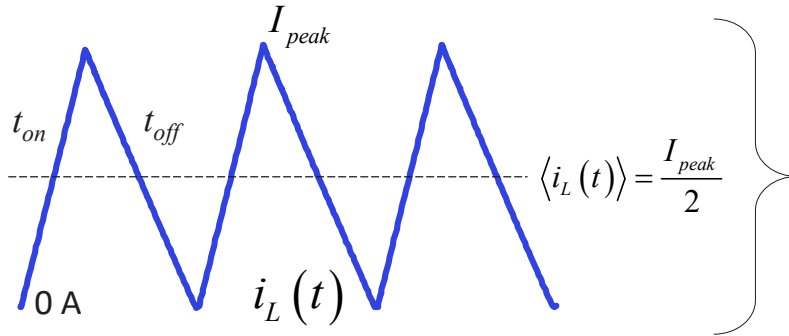
$V_{in} = 230 \text{ V rms} - \text{THD} = 2.7\%$

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Constant On-Time Control

- Voltage-mode control offers the easiest implementation for BCM PFCs
- Start with the inductor instantaneous current waveform:



$$p_{in}(t) = v_{in}(t) i_{in}(t) = v_{in}(t) \frac{i_{L,peak}(t)}{2}$$

$$i_{L,peak}(t) = \frac{v_{in}(t)}{L} t_{on}(t) \quad \rightarrow \quad p_{in}(t) = \frac{v_{in}^2(t)}{2L} t_{on}(t)$$

$$\langle i_{in}(t) \rangle = \frac{v_{in}(t)}{2L} t_{on}(t) \quad \leftrightarrow \quad \langle i_{in}(t) \rangle = \frac{v_{in}(t)}{R_{in}} = \frac{v_{in}(t)}{\frac{V_{ac}^2}{P_{in}}}$$

Resistive input

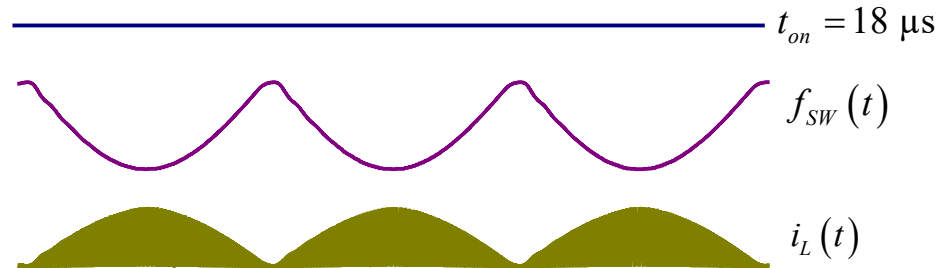
- The power sets the on-time value in relationship with the rms input voltage

$$t_{on} = \frac{2LP_{in}}{V_{ac}^2}$$

$\rightarrow i_{in}(t) = \frac{V_{ac} \sqrt{2t_{on}}}{2L} \sin(\omega t)$

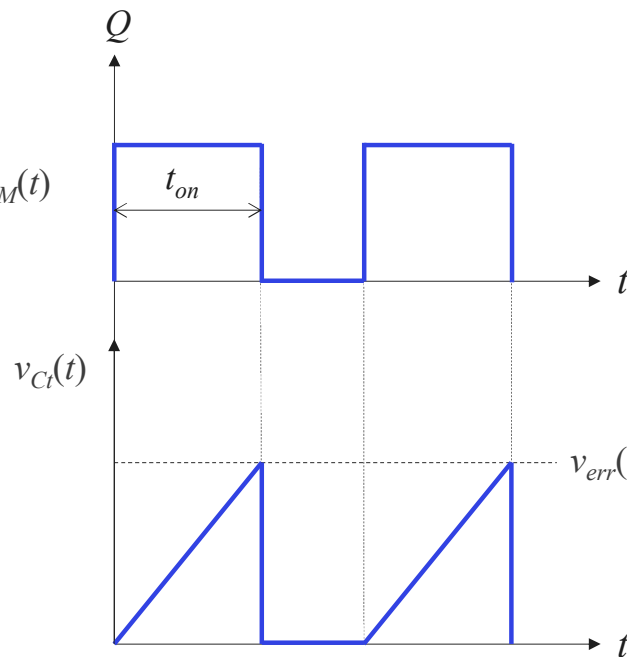
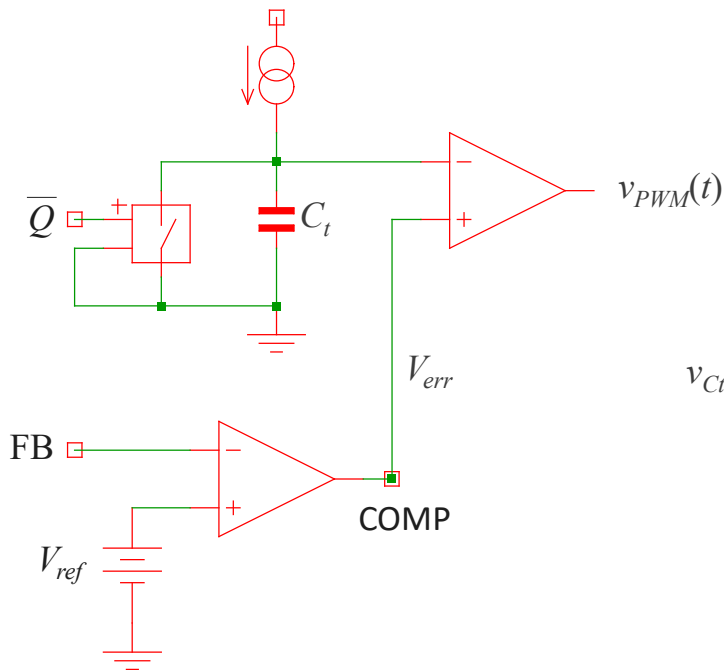
constant

- On-time is constant
- Frequency is variable



Modulating the On-Time

- A capacitor is charged by a constant-current source
- ✓ The error voltage modulates the toggling threshold and adjusts t_{on}



- ✓ A maximum on-time clamp limits the power
- ✓ This clamp can be adjusted based on the line level
- ✓ Modulation around the 0-V input improves distortion

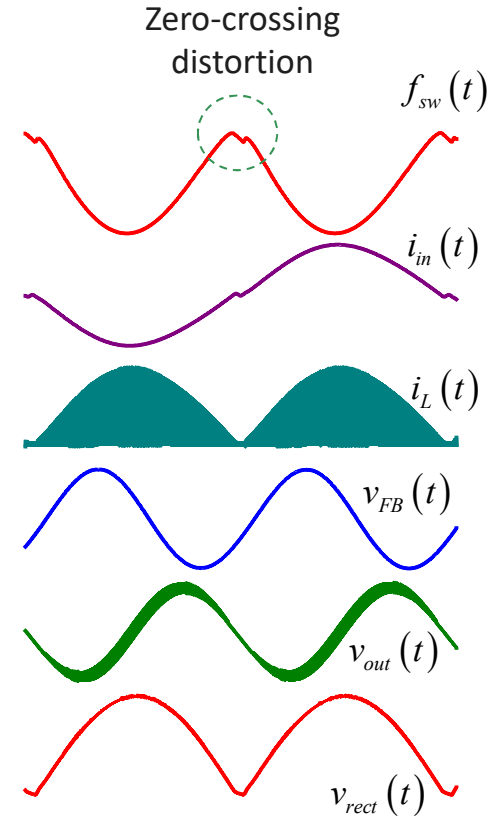
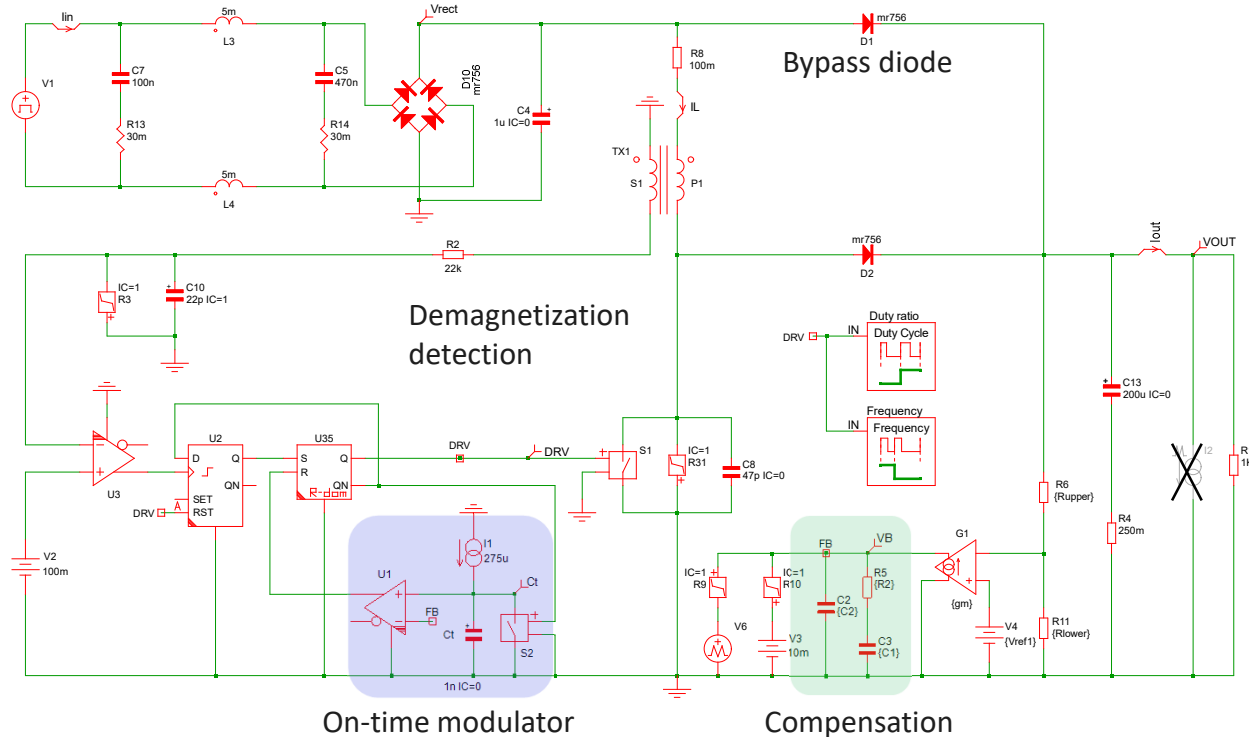
P_{out} increases



P_{out} decreases

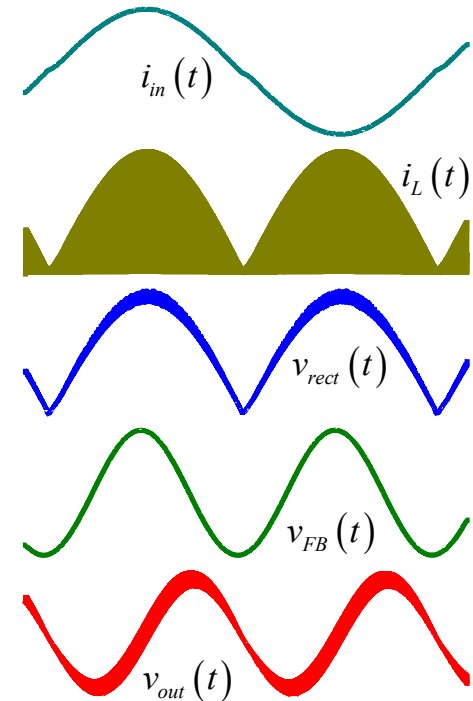
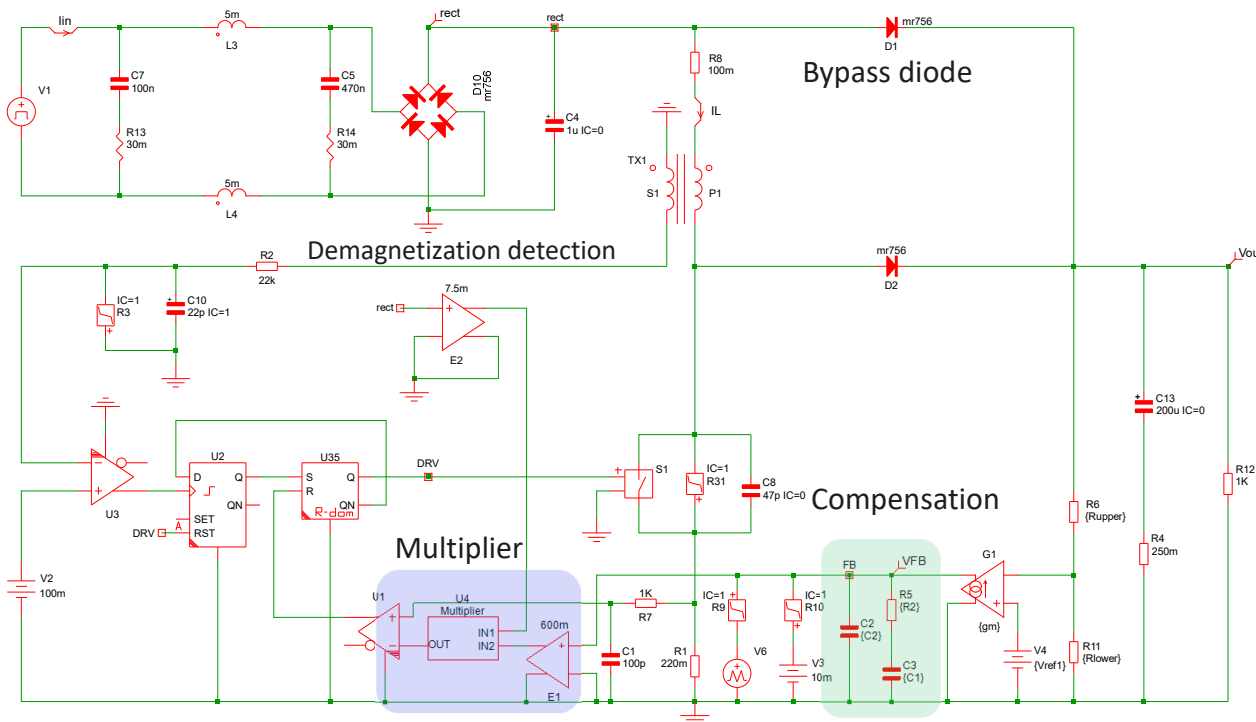
Voltage-Mode Operation

- Constant on-time can be implemented in voltage-mode control
- ✓ No need to sense the input voltage!



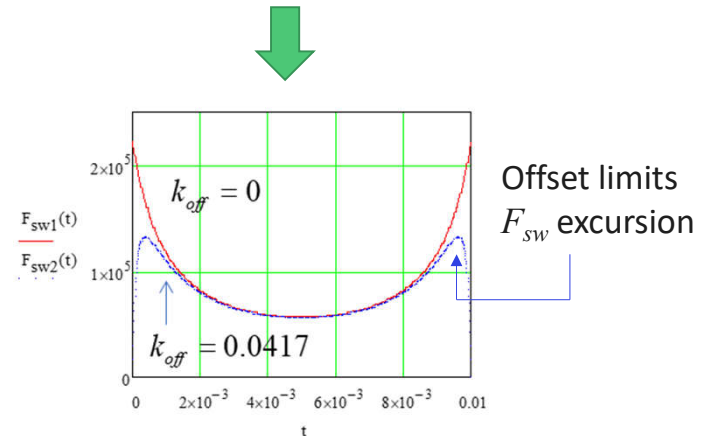
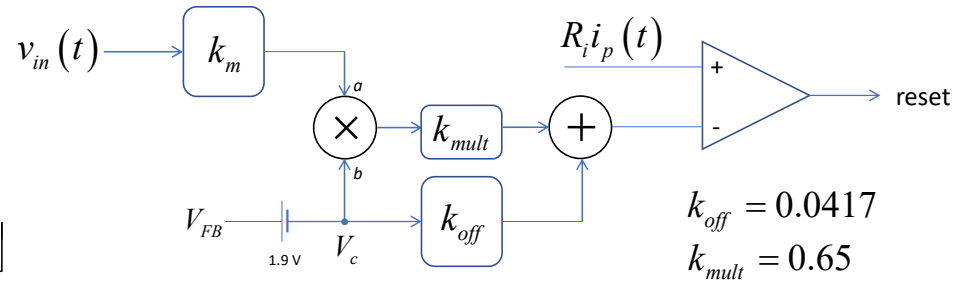
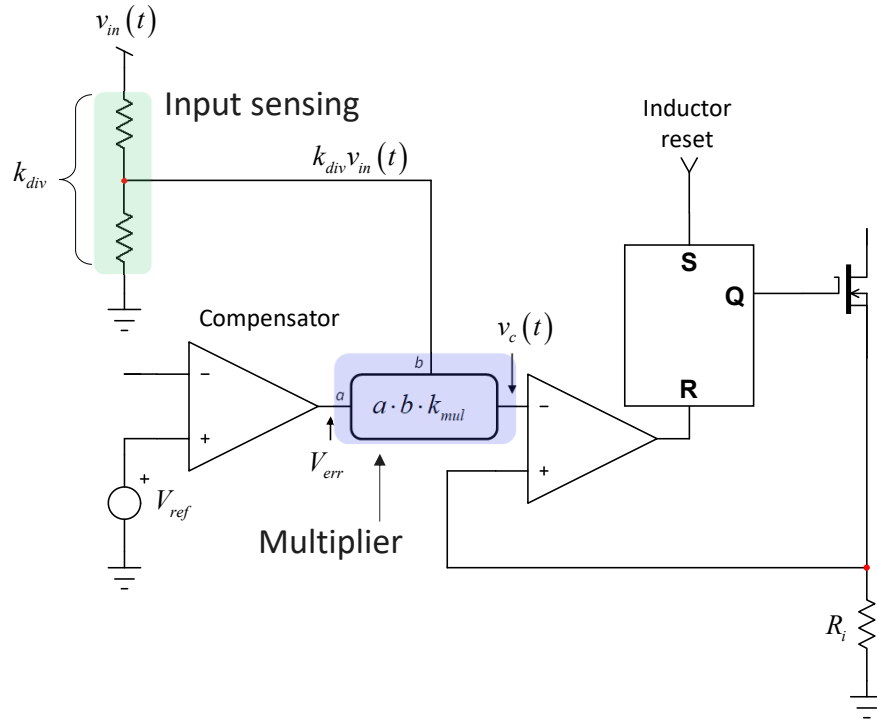
Peak-Current-Mode Operation

- The inductor *peak current* follows the rectified voltage for a sinusoidal envelope
- A multiplier is needed to sense the input voltage: increased power consumption



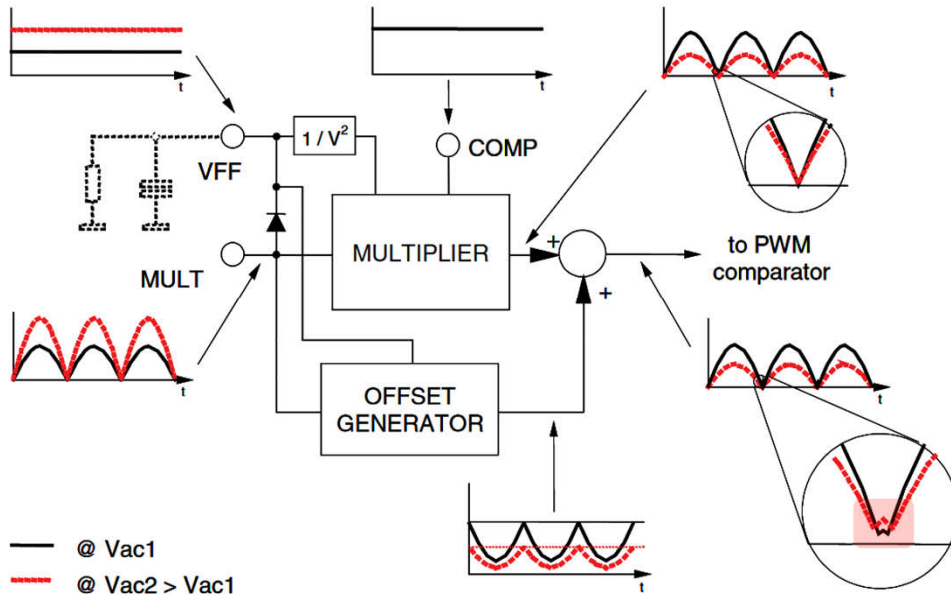
A Multiplier in the Chip

- The inductor current is scaled by the rectified voltage and follows the envelope
- A small offset is added to the multiplier and effectively reduces F_{sw} near 0 V

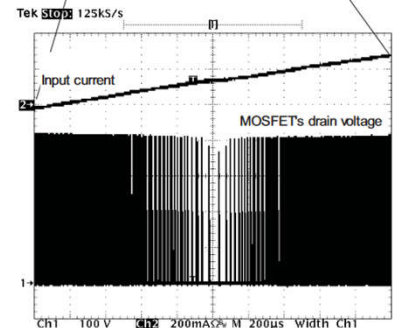
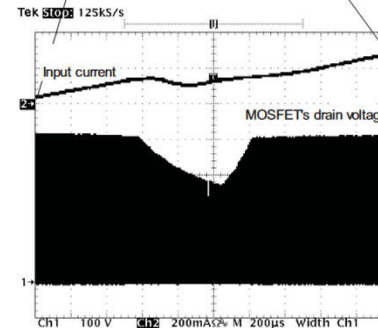
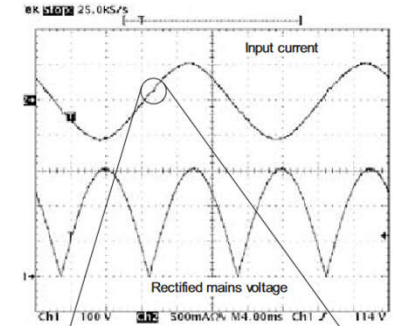
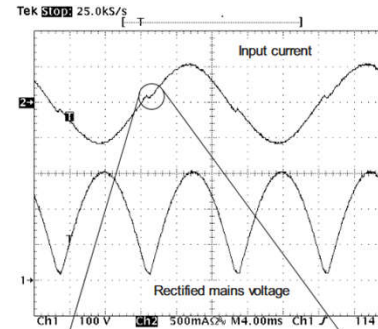


Harmonic Distortion Enhancer

- The front-end capacitor holds some residual voltage near zero crossing
- A THD enhancer typically forces a higher on-time at low input voltage

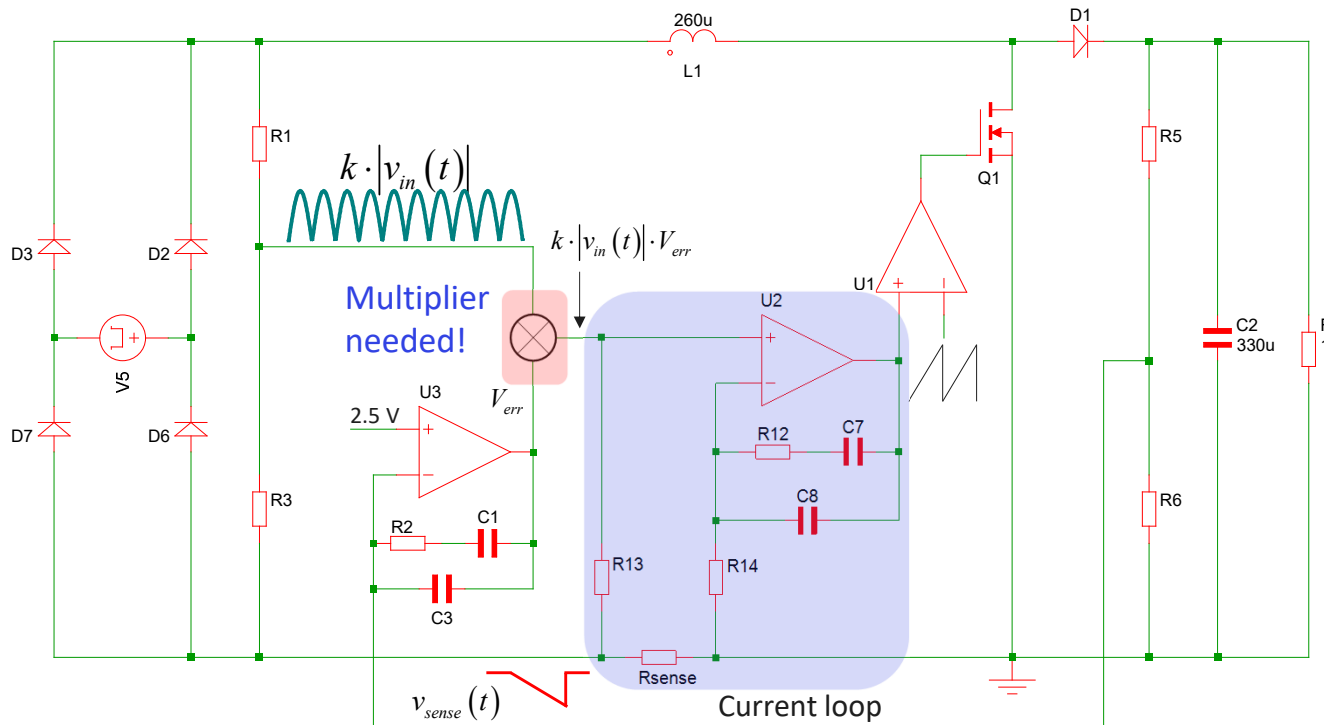


Front-end capacitor does not discharge to 0 V



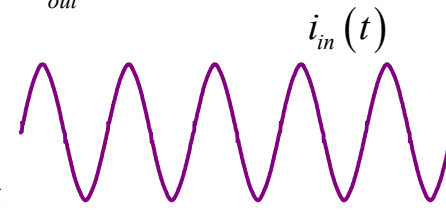
Average Mode Current

- The inductor current is shaped by a dedicated high-bandwidth loop
- ✓ Error between the inductor current and setpoint is minimized for best distortion



$$V_{in} = 100\text{ V rms}$$

$$P_{out} = 1\text{ kW}$$

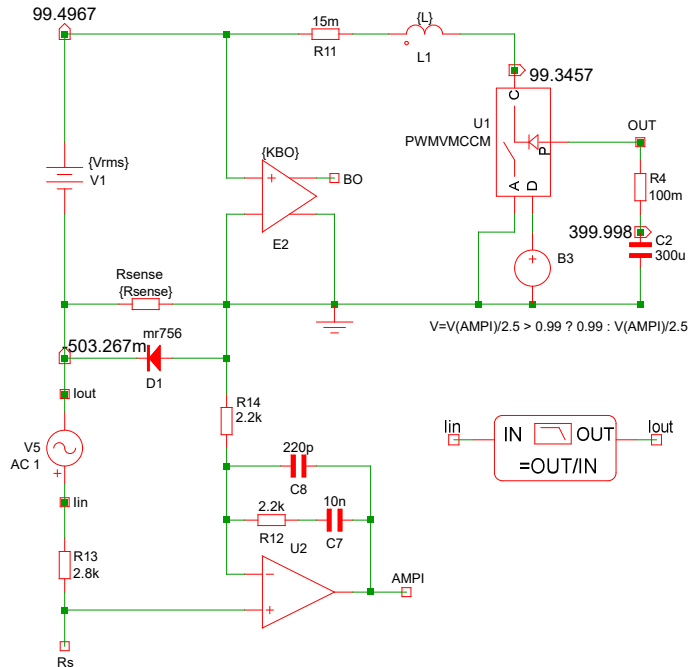


$$\text{THD} = 2.3\% V_{in} = 100\text{ V rms}$$

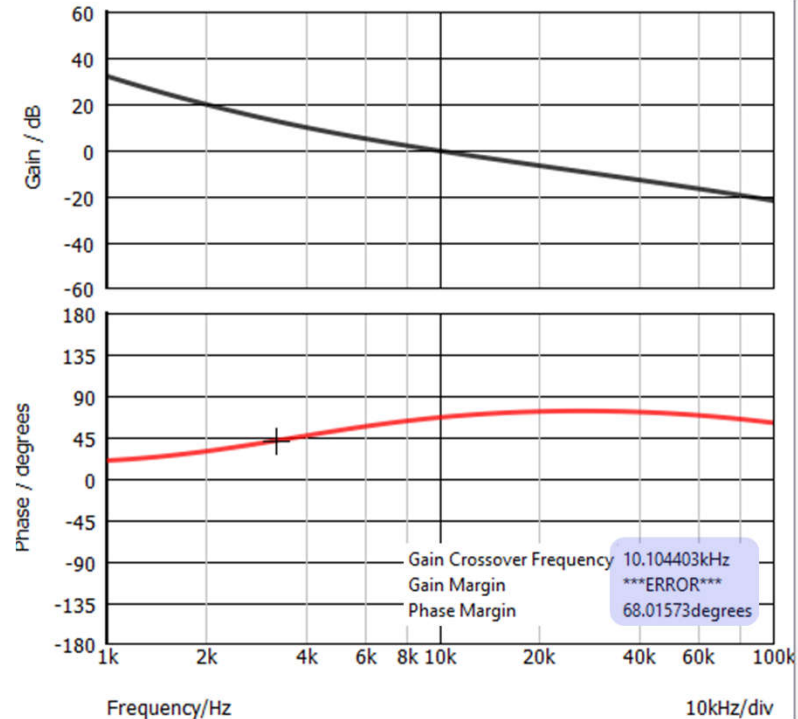
$$\text{THD} = 2.9\% V_{in} = 230\text{ V rms}$$

A High-Speed Current Loop

- It is important to ensure the fast and precise tracking of the current envelope
- ✓ The current loop must exhibit a wide bandwidth, e.g. 10 kHz typically

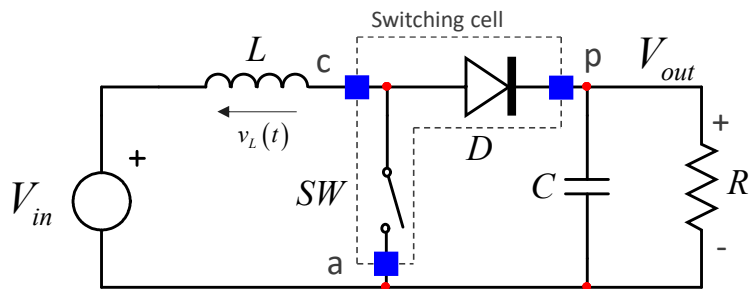


From control circuitry



Predictive Power Factor

- Most of the PFC circuits do sense the input voltage to build the control law
- ✓ Predictive timing generates PWM control without high-voltage sensing



$$\langle v_L(t) \rangle = 0 \quad \longrightarrow \quad \langle v_c(t) \rangle = V_{in}$$

$$\langle v_c(t) \rangle = V_{out} (1 - D) = V_{out} D_{off}$$

$$\longrightarrow V_{in} = V_{out} D_{off}$$

➤ The input current is the inductor current

$$i_{in}(t) = i_L(t) \quad \longrightarrow \quad \langle i_{in}(t) \rangle = \langle i_L(t) \rangle$$

Depends on power

$$\frac{\langle v_{in}(t) \rangle}{\langle i_{in}(t) \rangle} = \frac{V_{out}}{\langle i_L(t) \rangle} D_{off} \quad \longrightarrow \quad D_{off} = \frac{R_e}{V_{out}} \langle i_L(t) \rangle$$

Input resistance R_e

Regulated output

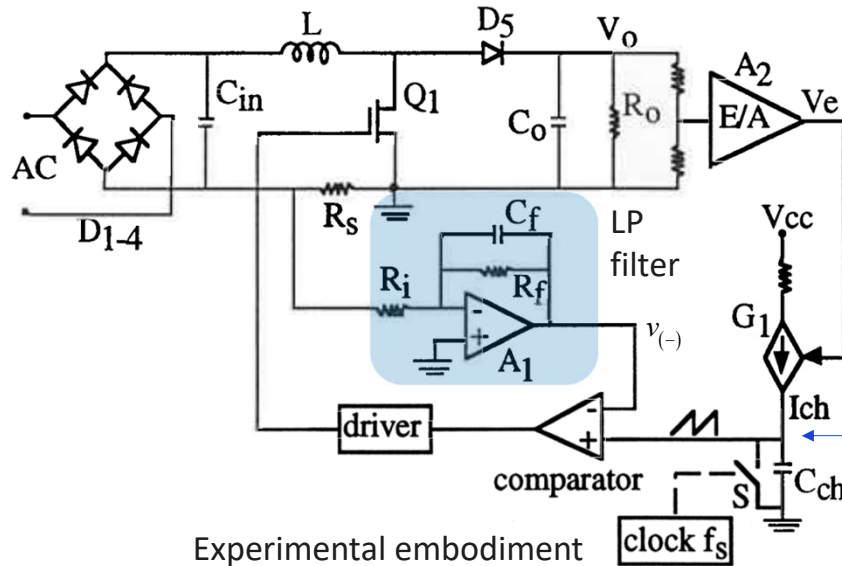
➤ Set the control law to program $D_{off}(t)$

$$D_{off}(t) = \frac{R_e}{V_{out}} \langle i_{in}(t) \rangle \quad d_{off}(t) = \left(\frac{R_e}{V_{out}} \right) \frac{|v_{in}(t)|}{R_e}$$

Average values Instantaneous variables

No Input Voltage Sensing

- By modulating the off-time duration across the input line, resistive input is ensured
- The input current is sensed via a shunt and averaged through a low-pass filter
- ✓ The error voltage adjusts the capacitor charging current and hence off-time duration



$$I_{ch} = g_m V_e$$

$$v_{(+)}(t) = \frac{I_{ch}}{C_{ch}} t = \frac{g_m V_e}{C_{ch}} t$$

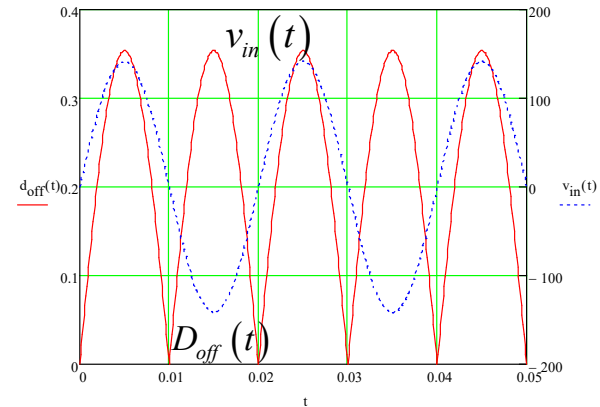
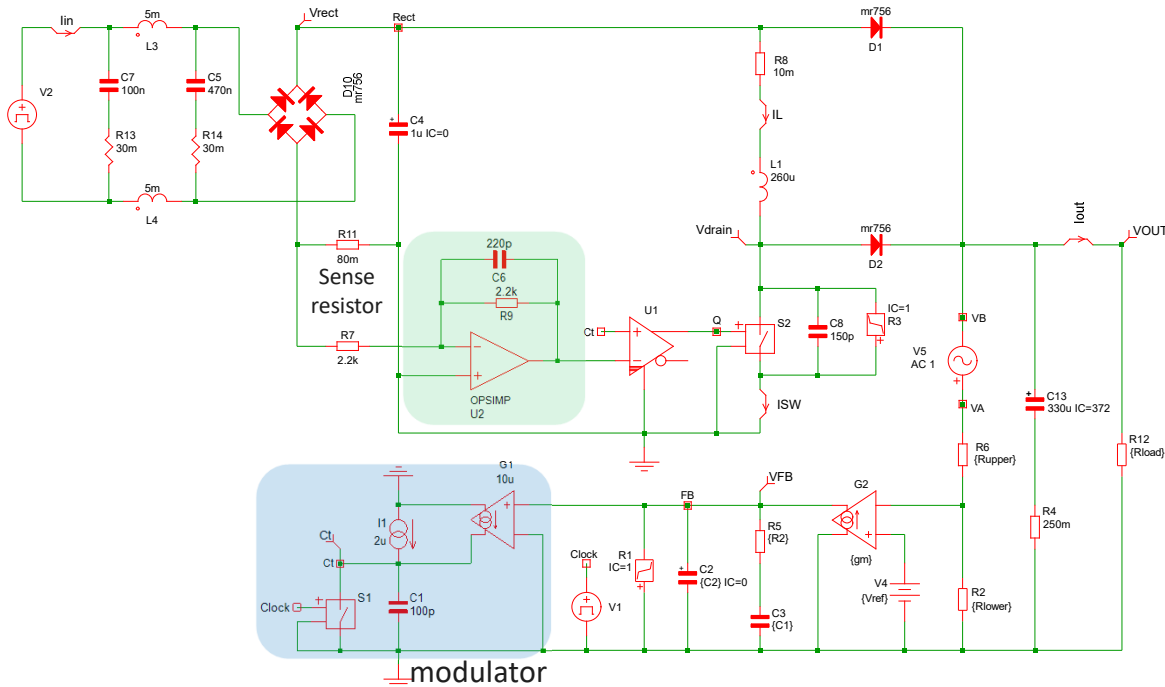
$$v_{(-)}(t) = \langle i_L(t) \rangle R_s$$

$$v_{(+)} = v_{(-)} \xleftrightarrow{\text{toggling}} \frac{g_m V_e T_{off}}{C_{ch}} = \langle i_L(t) \rangle R_s$$

$$D_{off}(t) = \frac{\langle i_L(t) \rangle R_s C_{ch}}{V_e g_m T_{sw}}$$

Simulation Example

- The application circuit is simple and requires a specific off-time modulator
- A dedicated amplifier shapes the negative input current via a shunt

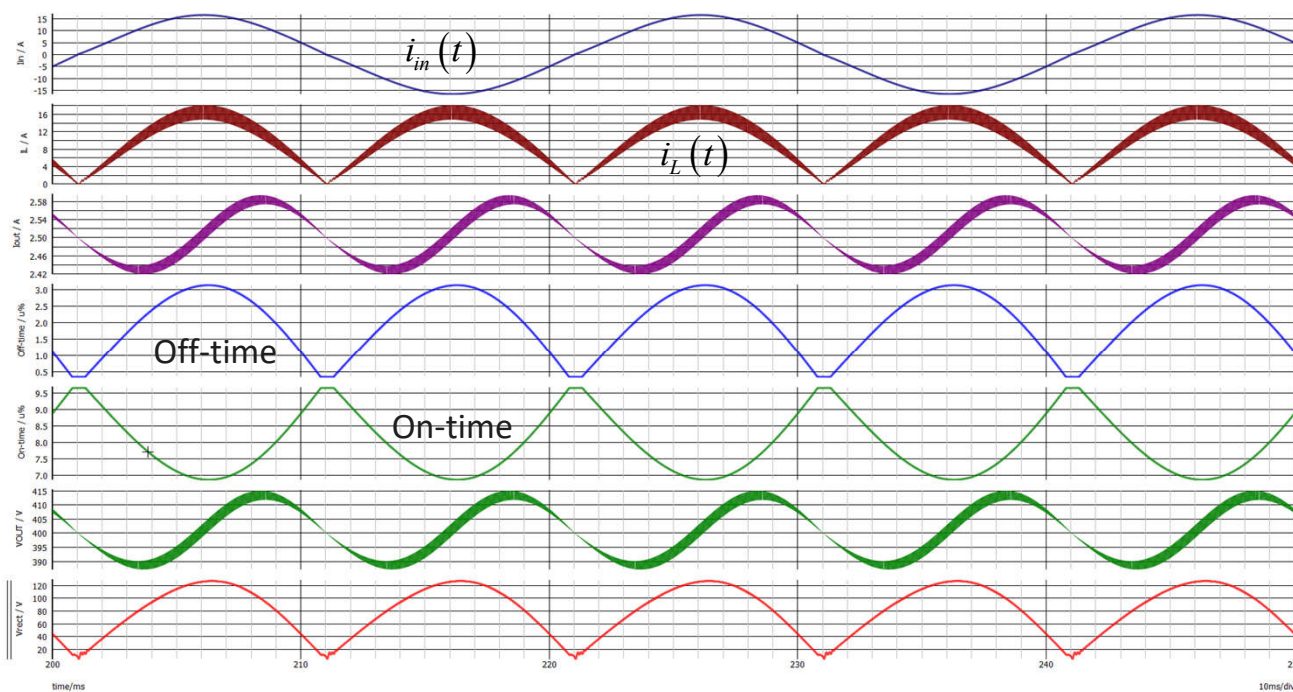


✓ The average off-time is modulated along the input sinewave

Simulation Results

- The input current waveform is perfectly sinusoidal and undistorted

$V_{in} = 100 \text{ V rms}$, $P_{out} = 1 \text{ kW}$



Distortion data:

$P_{out} = 1 \text{ kW}$

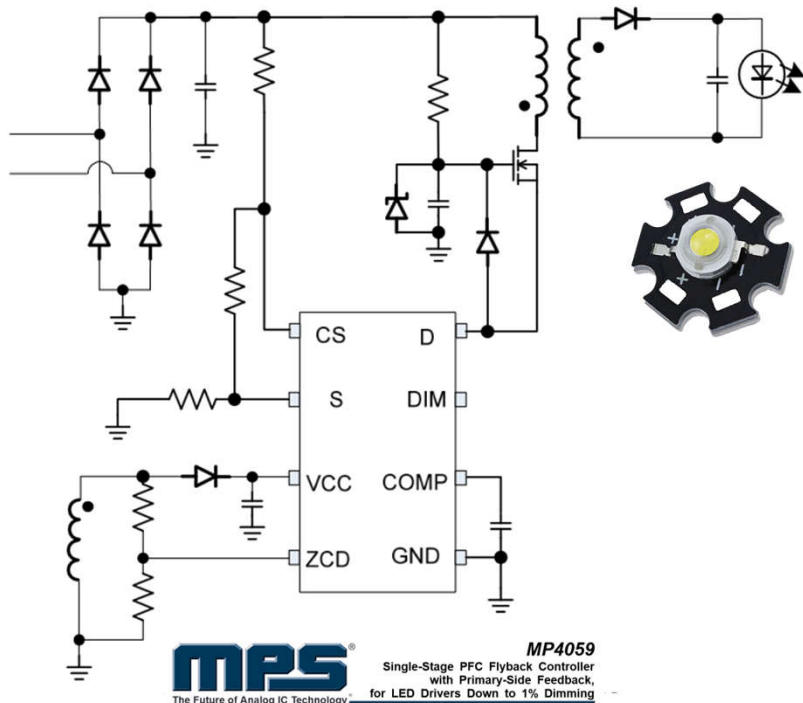
$V_{in} = 100 \text{ V rms}$ THD = 3%

$V_{in} = 230 \text{ V rms}$ THD = 6%

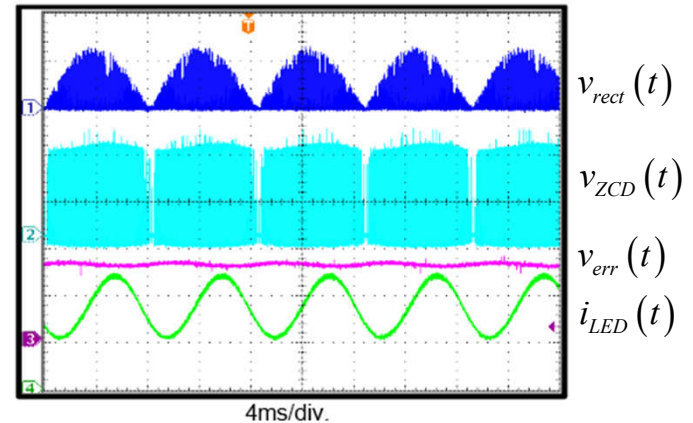
Regulated
output voltage

Single-Stage Converter

- It is possible to combine a PFC function with a flyback converter
- Very popular in lighting applications where bandwidth is naturally low



- ✓ Operates in quasi-resonant mode
- ✓ Power factor is usually greater than 0.9
- ✓ Constant on-time voltage-mode operation



Typical operating waveforms – 120 V rms

Agenda

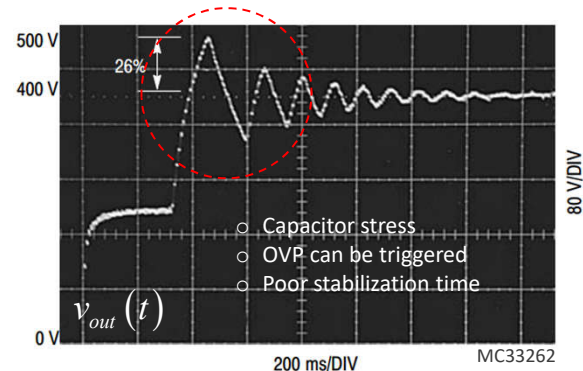
- Notions of Power Factor
- Power Factor Correction Structures
- Processing the Power
- Loop Compensation of a PFC
- Solutions from Future Suppliers

The Need for Stability

- A PFC is usually a boost converter operated in different conduction modes:
 - Continuous Conduction Mode or CCM: high-power system, usually > 300 W
 - Boundary/Borderline Conduction Mode or BCM: small to moderate power < 300 W
 - Many derived structures like interleaved or totem-pole for higher power levels
- The PFC controller implements a control law: how to force a sinusoidal input current?
 - In BCM converters, it is usually a constant on-time control, voltage- or current-mode
 - In CCM, there are usually proprietary control laws optimizing distortion and efficiency

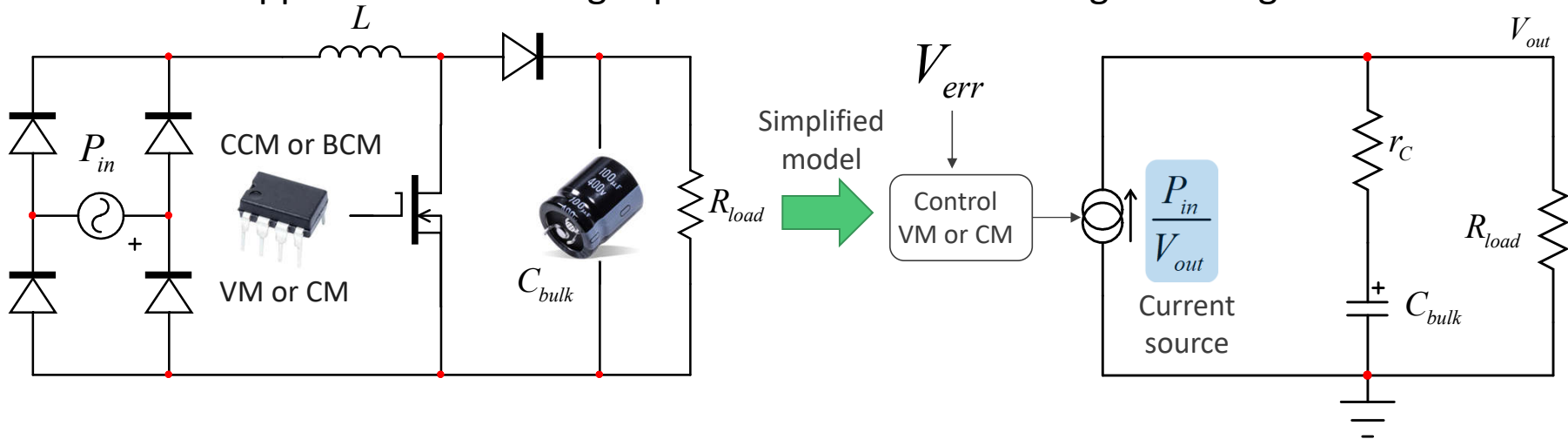


Regardless of the implementation, loop analysis is important to guarantee a stable and reliable operation



Modeling a Power Factor Correction Stage

- Several ways exist to model switching converters
- ✓ State-space averaging (SSA), PWM switch model, 1st-order approximation etc.
- A PFC is a slow system in essence with crossover frequency below 10 Hz
- ✓ 1st-order approximation averages power without considering switching mechanism



- If the load is a regulated switching converter, the incremental resistance is negative

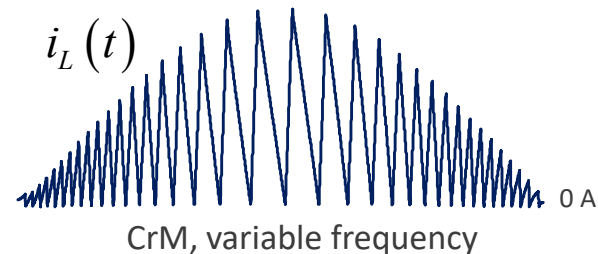
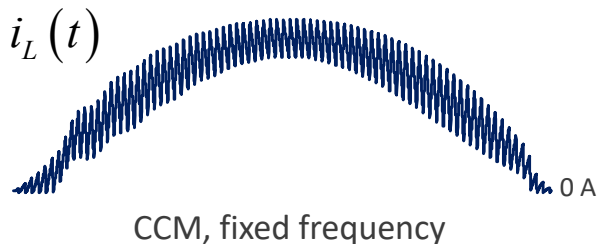
A General Formula to Express the Output Power

- A generic PFC control law obeys the following formula:

$$P_{in,avg} = \frac{K \cdot V_{in,rms}^m \cdot V_{control}}{V_{out}^n}$$

- ✓ m characterizes the input-voltage feed-forward
- ✓ n is 1 in general for predictive-sensing stages
- ✓ K is a constant which depends on the modulator, L , R_{sense} etc.

- ✓ This is a large-signal expression which needs to be linearized
- ✓ The corresponding model does not predict high-frequency phenomenon like RHPZ
- ✓ Perfect for low-frequency approach of a naturally-slow PFC stage
- Works for any type of operation, CCM, CrM/BCM, fixed or variable frequency etc.



Example with CrM Power Factor Correction

- The power transmitted by a power stage operated in CrM obeys the formula:

$$P_{in,avg} = \frac{V_{ac}^2}{2L} G_{PWM} V_{err}$$

- ✓ constant on-time voltage-mode control
- ✓ G_{PWM} represents the modulator small-signal gain
- ✓ L is the boost inductor value



NCP1608
NCP1622
L6562
L6564
MP44019
MP44018



100% efficiency



$$P_{in} = P_{out}$$

$$I_{out} = \frac{V_{ac}^2}{2L V_{out}} G_{PWM} V_{err}$$

Nonlinear expression!

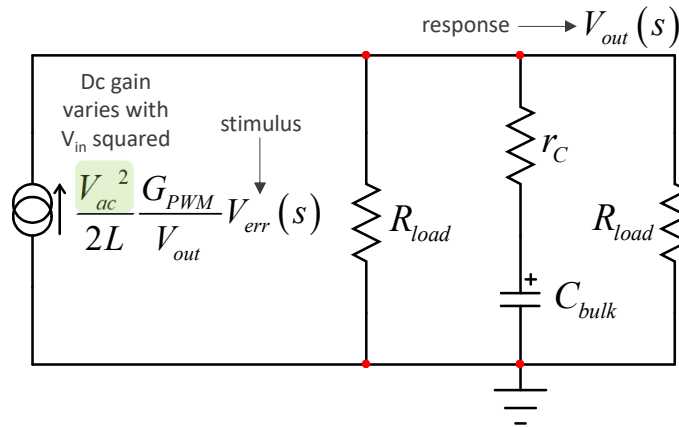
- Run partial differentiation to obtain small-signal coefficients:

$$\hat{i}_{out} = \frac{\partial}{\partial V_{out}} \left(\frac{V_{ac}^2}{2L} \frac{G_{PWM} V_{err}}{V_{out}} \right) \Bigg|_{\hat{v}_{err}=0} \hat{v}_{out} + \frac{\partial}{\partial V_{err}} \left(\frac{V_{ac}^2}{2L} \frac{G_{PWM} V_{err}}{V_{out}} \right) \Bigg|_{\hat{v}_{out}=0} \hat{v}_{err}$$



Modeling a Power Factor Correction Stage

- From the small-signal equation, build the complete simplified model



ESR contribution high frequency only

$$H(s) = H_0 \frac{1 + \frac{s}{\omega_z}}{1 + \frac{s}{\omega_p}} \approx H_0 \frac{1}{1 + \frac{s}{\omega_p}}$$

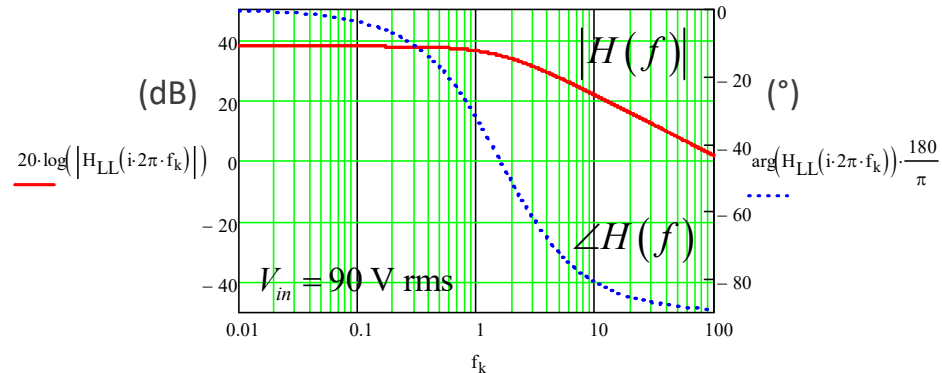
$$H_0 = \frac{V_{ac}^2}{4L} \frac{R_{load} G_{PWM}}{V_{out}} \quad \omega_p \approx \frac{2}{R_{load} C_{bulk}}$$

- Assume the following specifications:

$$\left. \begin{aligned} P_{in} &= 144 \text{ W} \\ V_{out} &= 380 \text{ V} \\ L &= 250 \mu\text{H} \\ C_{bulk} &= 200 \mu\text{F} \\ R_{load} &= 1 \text{ k}\Omega \end{aligned} \right\}$$

$$\begin{aligned} H_0 &= 78 \approx 38 \text{ dB} \\ f_p &\approx 1.6 \text{ Hz} \end{aligned}$$

Plot
power stage (LL)




Compensation Strategy for the PFC

- Without specific treatment, dc gain changes with line input squared
- For ratio of 2.3 between 265 V and 90 V rms input, gain changes by $2.94^2 \approx 9$
- Select a crossover $f_c = 50$ Hz at a 265-V input to keep at least 8-10 Hz at lowest line

$$|H(f_c)| = \frac{H_0}{\sqrt{1 + \left(\frac{f_c}{f_p}\right)^2}} = 26.6 \quad \text{gain excess}$$

↑
50 Hz

Go for a

 type 2

$$\angle H(f_c) = -\tan^{-1}\left(\frac{f_c}{f_p}\right) = -88^\circ$$

↑
50 Hz

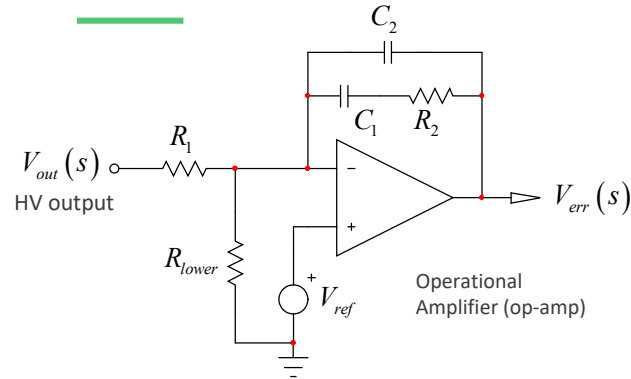
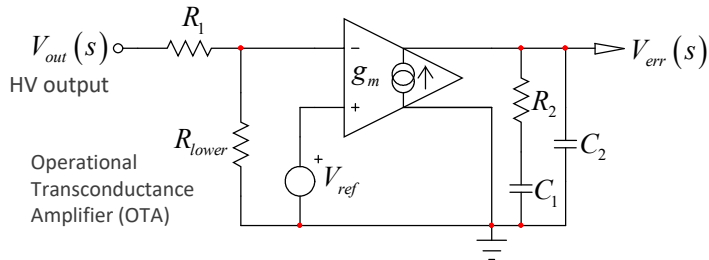
- Bring a $1/26.6$ or 28.5-dB attenuation at 50 Hz
- For a 70° phase margin, boost the phase by:
 $boost = 70^\circ - (-88) - 90 = 68^\circ$
- One pole and one zero to boost the phase by 68°
- $f_p = 260$ Hz
- $f_z = 9.6$ Hz

$$G(s) = G_0 \frac{1 + \frac{\omega_z}{s}}{1 + \frac{s}{\omega_p}}$$

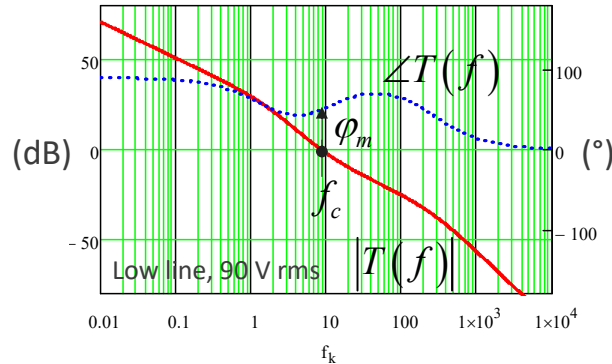
Type 2 compensator

Check Compensated Response

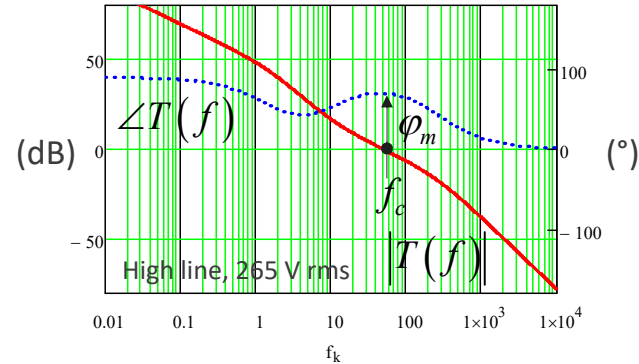
- A type 2 compensator is needed



- Check crossover and phase margin at the input line extremes $T(s) = H(s)G(s)$



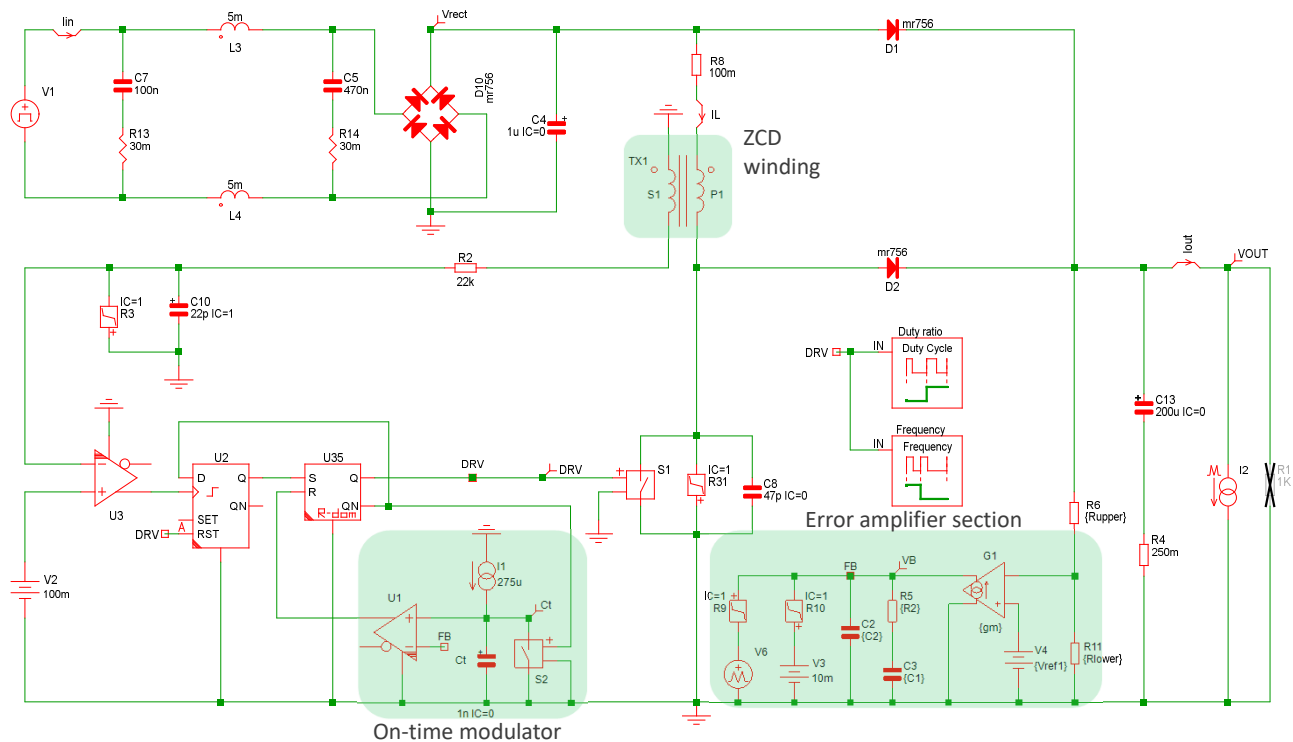
$$f_c = 8.5 \text{ Hz} \quad \varphi_m = 50^\circ$$



$$f_c = 50 \text{ Hz} \quad \varphi_m = 70^\circ$$

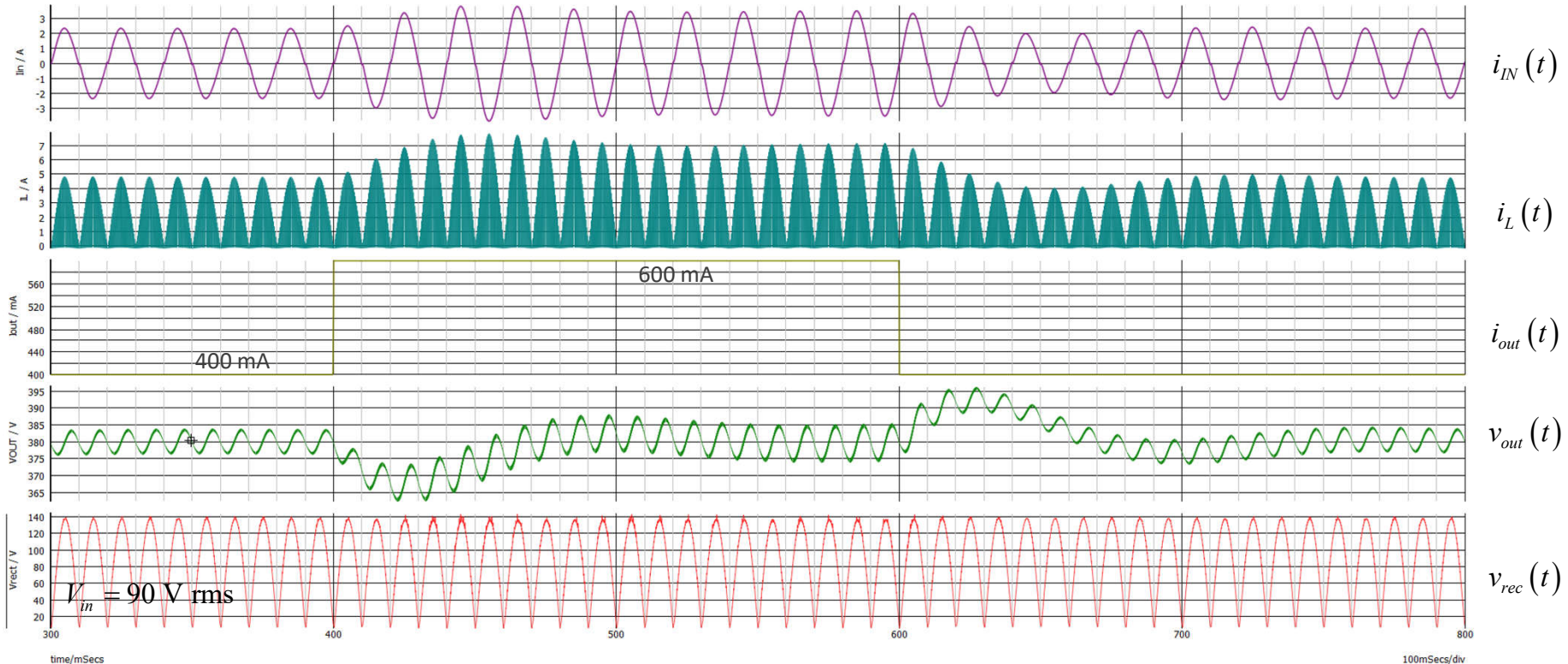
Simulate the Converter after Compensation

- SIMPLIS[®] is well suited for simulating power factor correction stages
- The program can plot the ac response from a switching circuit and simulates fast



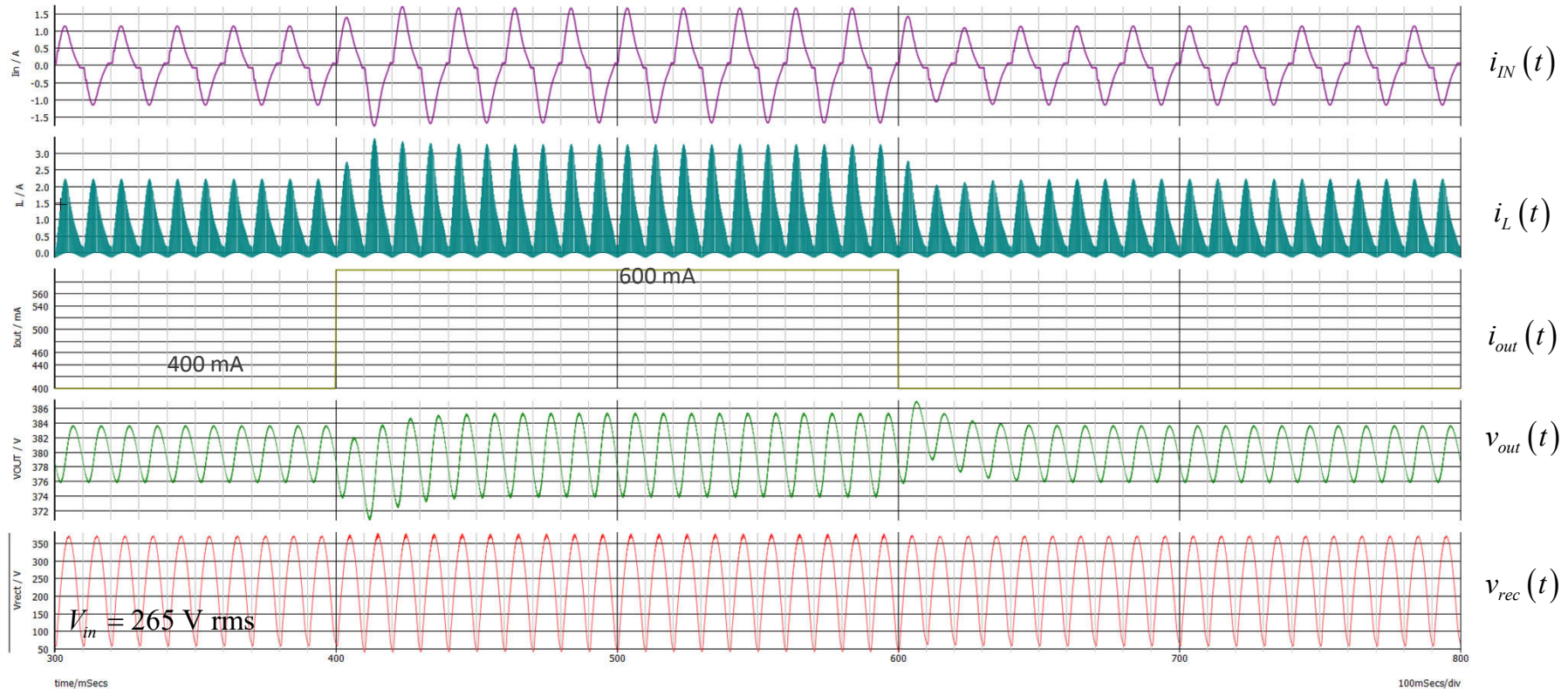
Check Transient Response is Acceptable

- The output current is stepped from 400 to 600 mA at the lowest 90-V rms input voltage



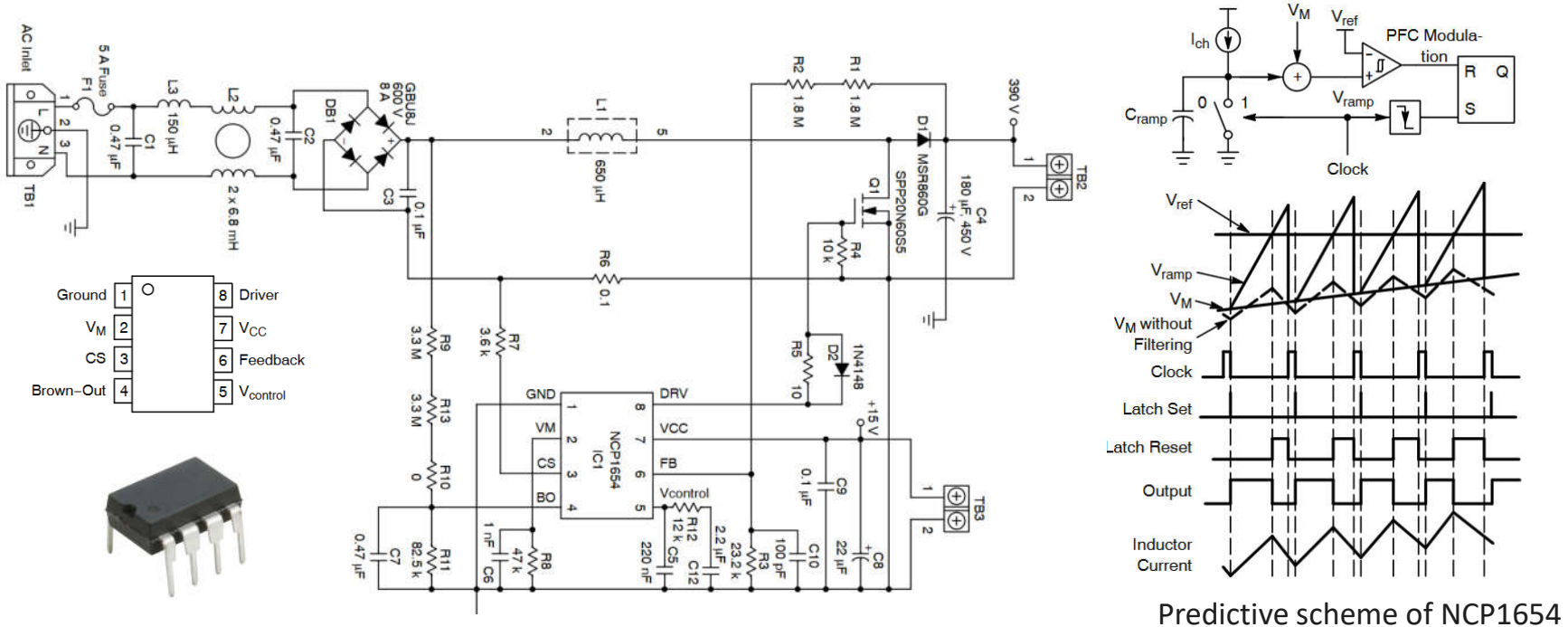
Transient Response at High Line

- In high-line conditions, the PFC is stable but given the higher crossover, distortion suffers



Compensating a CCM PFC

- We take the example of a 1-kW PFC operated in continuous conduction mode
- An averaged model is used to extract the control-to-output transfer function
- The predictive controller is the NCP1654 from **onsemi**.



Closing the Loop

- The control-to-output transfer function is obtained with an averaged SPICE model
- Some in-line behavioral equations describe the controller's internals
- ✓ Works in ac and transient analyzes

Automatic computation

```
.param gm=200u
.param boost={PM-PS-90}
.param G={10^(-Gfc/20)}
.param k={tan((boost/2+45)*pi/180)}
.param fp={fc*k}
.param fz={fc/k}

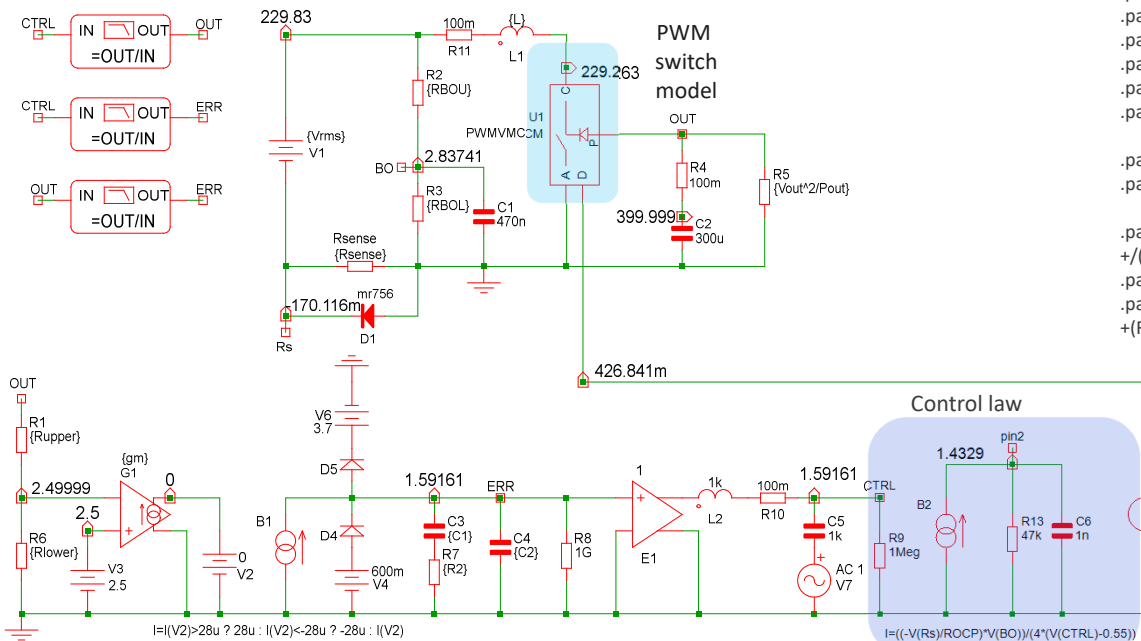
.param a={sqrt((fc^2/fp^2)+1)}
.param b={sqrt((fz^2/fc^2)+1)}

.param R2={{(a/b)*(fp*G)*(Rlower+Rupper)
+/(fp-fz)*Rlower*gm}}
.param C1={1/(2*pi*R2*fz)}
.param C2={{(Rlower*gm)/(2*pi*fp*G*
+(Rlower+Rupper))}/(b/a)}

.param Vrms=230
.param Vout=400
.param Pout=1.3k
.param L=54u

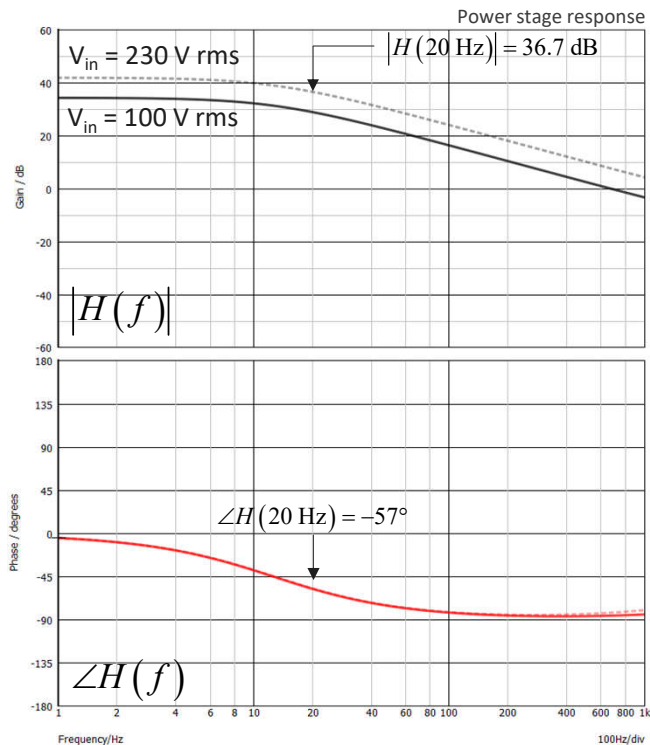
.param RBO=82.5k
.param ROCP=3.8k
.param Vp=2.5
.param Rsense=30m
.param Ib=100u
.param Rupper={{(Vout-2.5)/Ib}}
.param Rlower={{2.5/Ib}}

.param fc=20
.param Gfc=36.7
.param ps=-60
.param pm=60
```



The Power Stage Response

- The control-to-output transfer function is the starting point for compensation
- Infer a compensation strategy by reading information from magnitude and phase



- ✓ Crossover cannot be too high otherwise ripple may pollute the control voltage
- If too high then ripple will bring distortion and produce third harmonic
- Too low brings an unacceptable slow transient response
- ✓ Without feedforward the crossover may theoretically move with a factor of 9 in high- and low-line conditions
- ✓ NCP1654 feedforward limits the change in crossover frequency

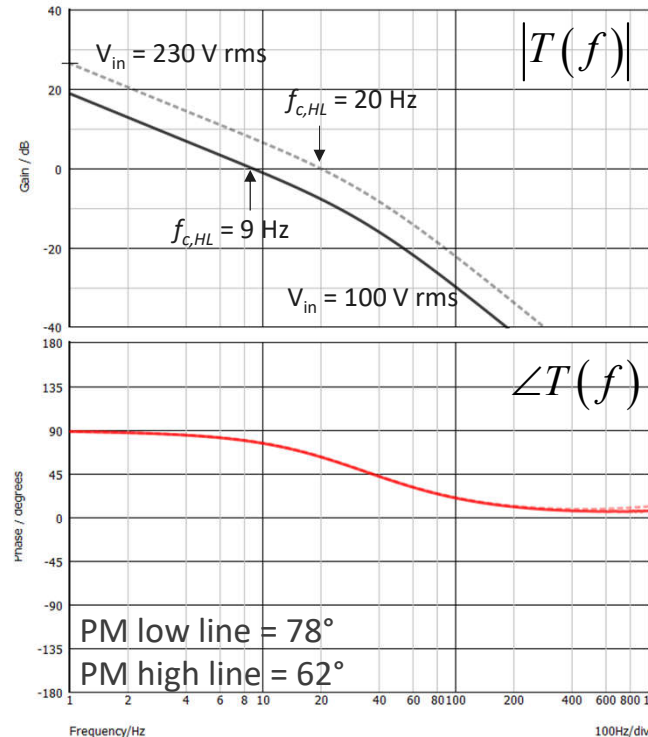
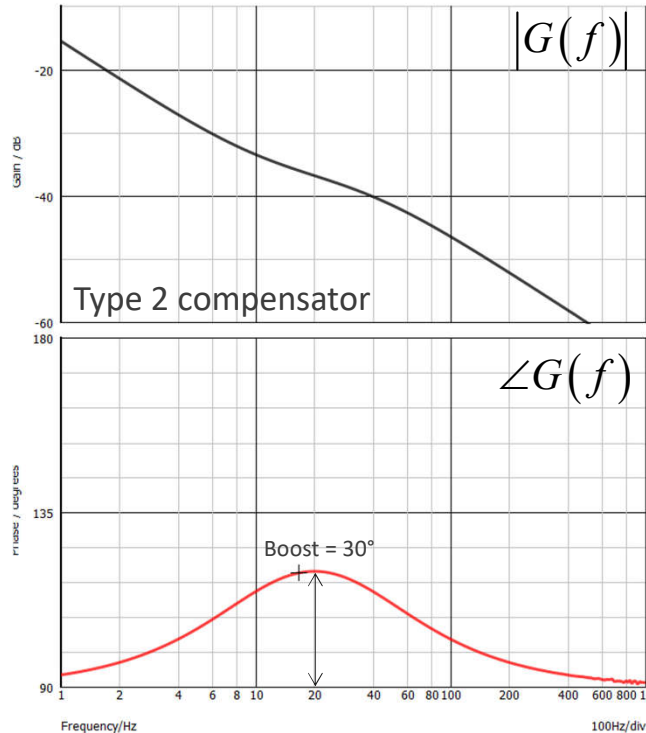


Select f_c in high-line conditions
to obtain 5-10 Hz at low line

$$f_{c,HL} = 20 \text{ Hz}$$

Check Loop Gain

- The dc input voltage in an ac analysis is the rms voltage of the source
- Enter 100 V dc and 230 V dc for respective low- and high-line simulations

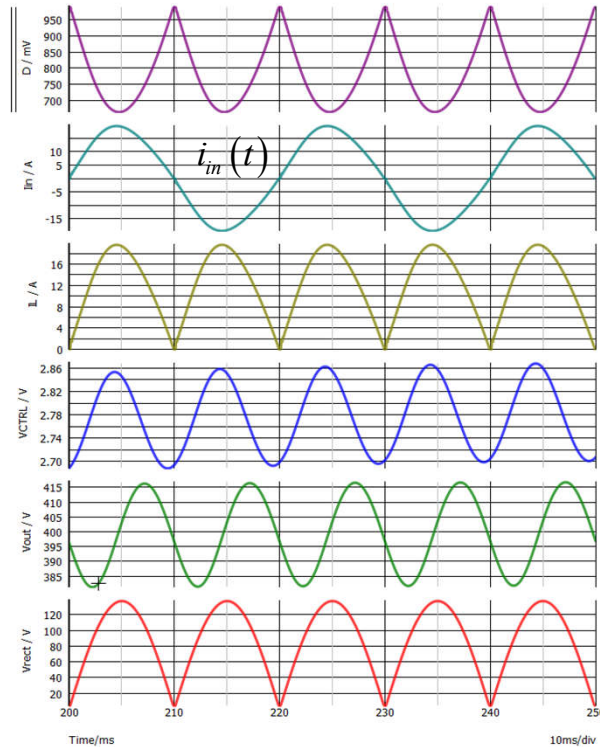


Computed values:

Vrms = 230
 Vout = 400
 Pout = 1.3k
 L = 54u
 RBOL = 82.5k
 RBOU = 6.6Meg
 ROCP = 3.8k
 Vp = 2.5
 Rsense = 30m
 Ib = 100u
 Rupper = 3.975Meg
 Rlower = 25k
 fc = 20
 Gfc = 36.7
 ps = -60
 pm = 60
 gm = 200u
 boost = 30
 G = 14.621771745m
 k = 1.73205080757
 fp = 34.6410161514
 fz = 11.5470053838
 a = 1.15470053838
 b = 1.15470053838
 R2 = 17.546126093k
 C1 = 785.54219388n
 C2 = 392.77109694n
 Compensator

Transient Response Performance

- The large-signal average model lends itself well to a transient simulation
- The input current at low line shows a good harmonic distortion figure of 4.2%

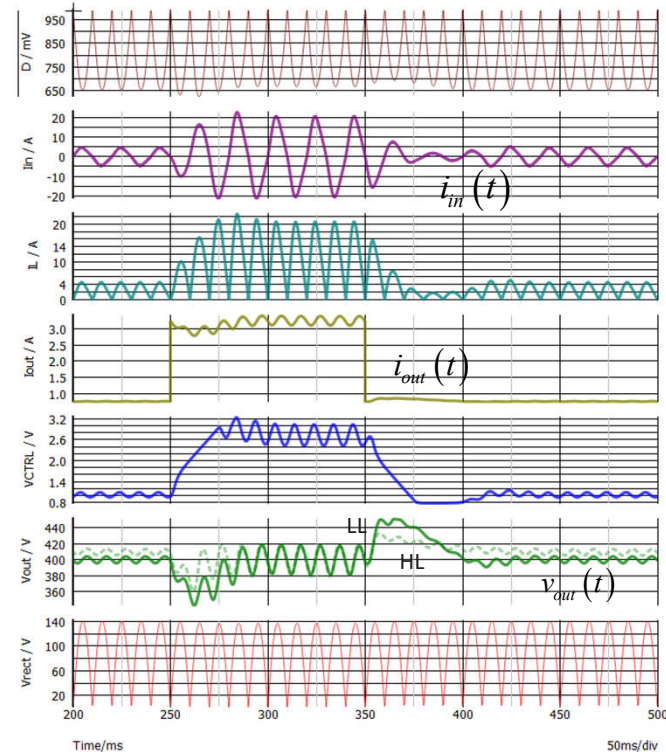


THD_{LL} = 4.23%
THD_{HL} = 6.33%

The output current is stepped from 300 W to 1.3 kW with a 1-A/μs slope

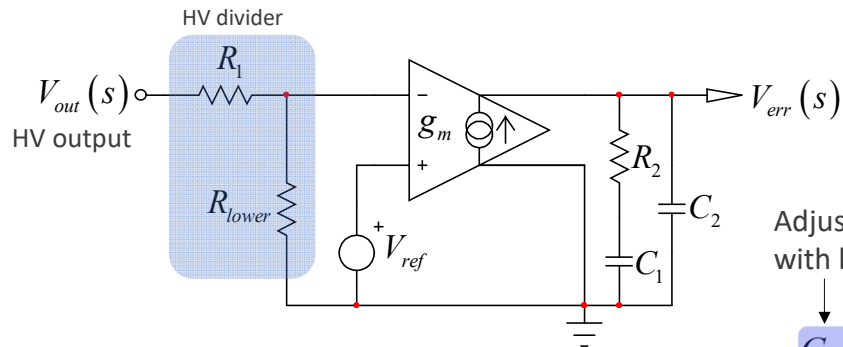


The transient response is stable at low and high line



Internal Digital Compensation

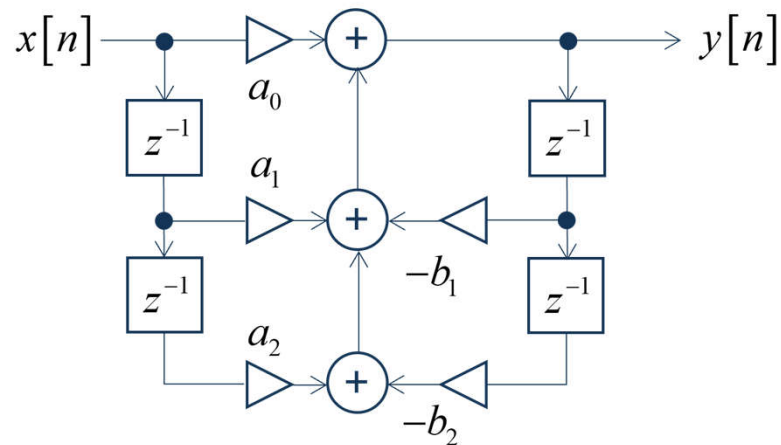
- The NCP1680 embeds an internal type 2 compensator
- A low-pass filter then follows to reduce the ripple contribution
- ✓ Mid-band gain is adjusted based on the input line value



$$G(s) = \frac{V_{err}(s)}{V_{out}(s)} = -G_0 \frac{1 + \frac{\omega_z}{s}}{1 + \frac{s}{\omega_p}}$$

Adjusted with line
 $G_0 \approx 13.6 \text{ dB}$
 $\omega_z \approx 1.44 \text{ Hz}$
 $\omega_p \approx 68 \text{ Hz}$

Type 2 compensator – analogue version

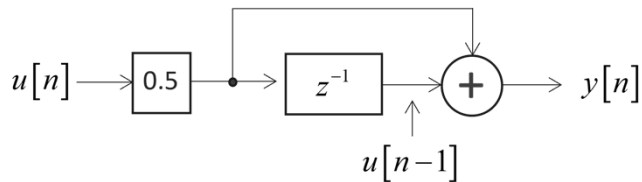


Digital implementation

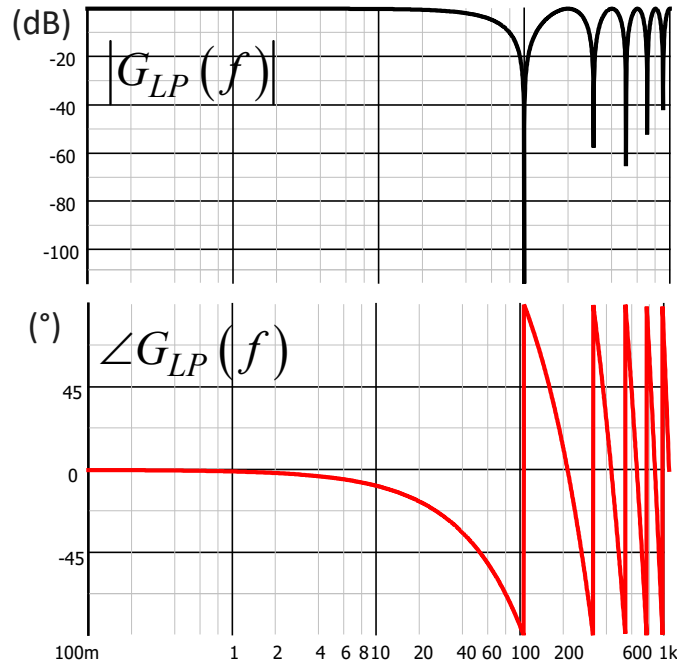
A Low-Pass Filter Reduces Feedback Ripple

- A low-pass filter is inserted in series with the compensator
- The digital implementation of this filter brings efficient output ripple rejection
- The sampling frequency is adjusted depending on the line frequency

$$y[n] = 0.5(u[n] + u[n-1])$$



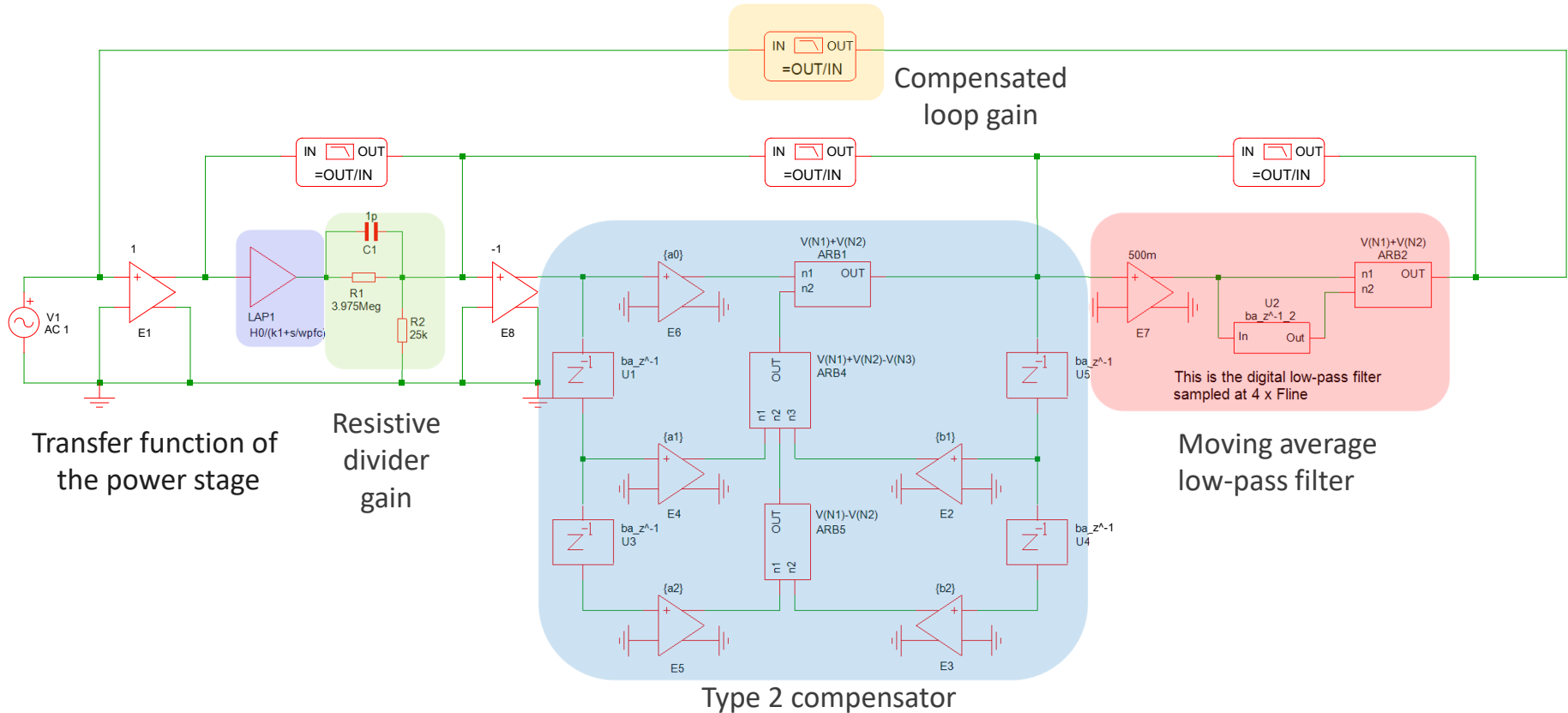
$$G(s) \approx \frac{1 + \frac{s}{\omega Q_N} + \left(\frac{s}{\omega}\right)^2}{1 + \frac{s}{\omega Q_D} + \left(\frac{s}{\omega}\right)^2}$$



- ✓ Sampling frequency is $4F_{line}$
- ✓ It sets a notch at twice the line frequency

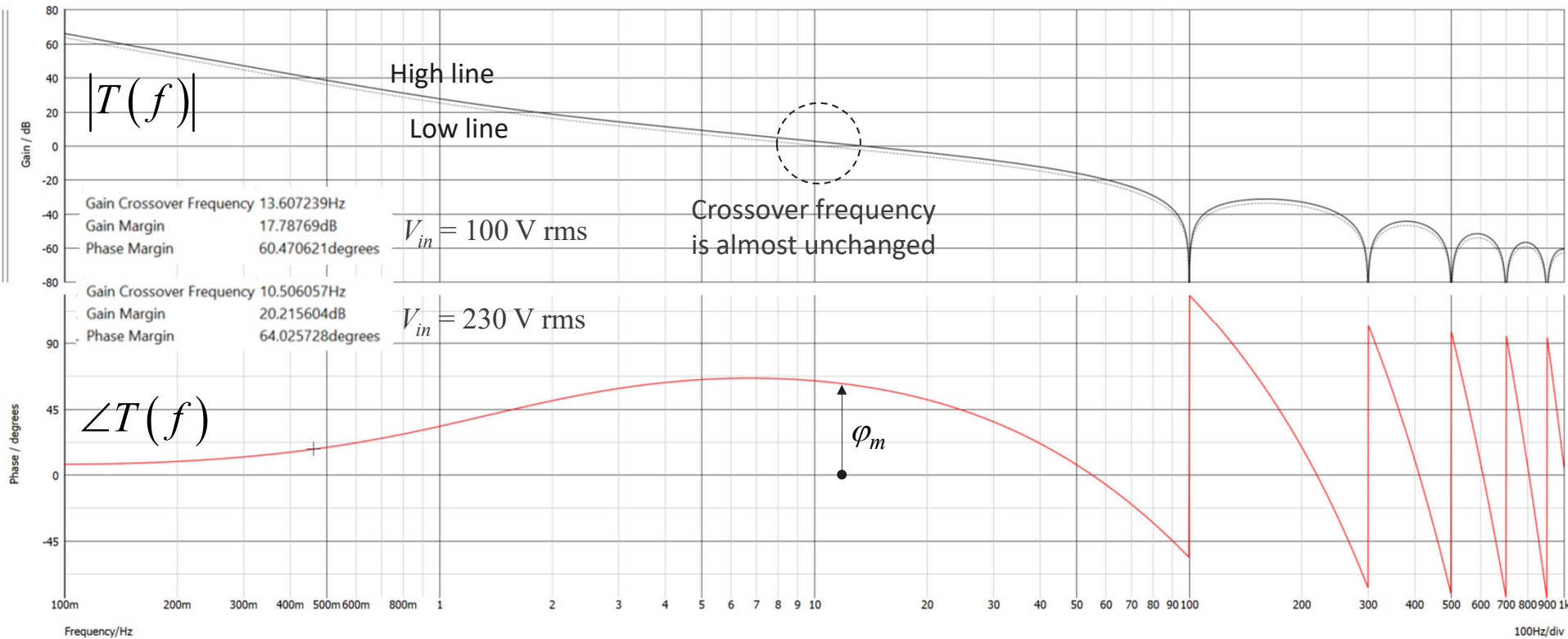
SIMatrix Compensated Simulation

- The digital filter is simulated with delay lines and fed by a Laplace expression



Typical Results for a 300-W Board

- The 300-W TPPFC features a constant crossover frequency regardless of input line



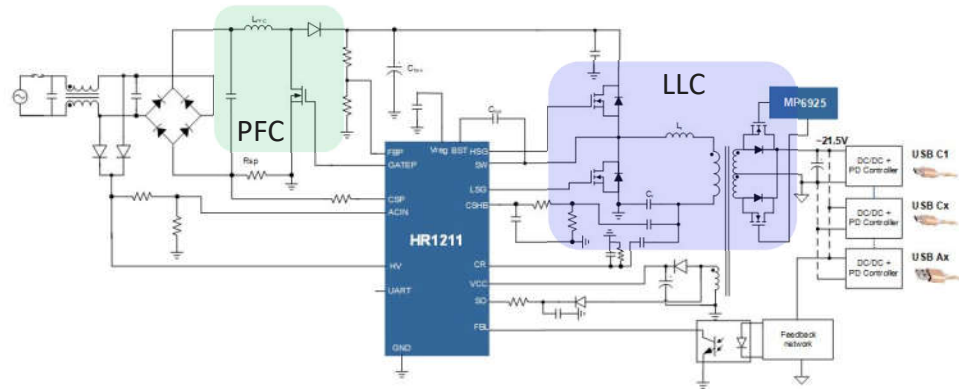
Agenda

- Notions of Power Factor
- Power Factor Correction Structures
- Processing the Power
- Loop Compensation of a PFC
- Solutions from Future Suppliers

Power Factor Controller Selection

- The selection of a PFC controller depends on various parameters:
- ✓ Constant on-time in BCM for low power, up to 200-300 W
- ✓ Want higher power in BCM: go for interleaved PFC
- ✓ Average mode control and CCM for high power, up to several kW
- ✓ Need for optimized efficiency? Go for multi-mode operation
- ✓ Need for the best efficiency? Go for a totem-pole PFC
- ✓ For compact design, go for a combo chip combining a PFC and a switching controller

- TEA2017: PFC and LLC 
- FAN6921BMR: PFC and QR flyback 
- IDP2308: PFC and LLC 
- STCMB1: PFC and LLC 
- HR1213: PFC and LLC 



PFC Controllers from **MPS**

Part-Number	Structure	Operating Frequency	Control Mode	Operating Mode	HV pin	Package
MP44018A	Boost	Variable	VM	BCM	—	SO-8
MP44019	Boost	Variable	VM	BCM	—	SO-8
MP44010	Boost	Variable	VM	BCM	—	SO-8
HR1213	Combo LLC	Variable Fixed	CM	CCM MM	√	SO-20
HR1210	Combo LLC	Variable Fixed	CM	CCM MM	√	SO-20
HR1211	Combo LLC	Variable Fixed	VM	CCM MM	√	SO-16

PFC Controllers from onsemi.

Part-Number	Structure	Operating Frequency	Control Mode	Operating Mode	HV pin	Package
NCP1623	Boost	Variable	VM	BCM	—	TSOP-6
NCL2801	Boost	Variable	VM	BCM	—	SO-8
NCP1654	Boost	Fixed	CM	CCM	—	SO-8
NCP1680	Totem-pole	Variable	VM	BCM	√	SO-16
NCP1681	Totem-pole	Variable Fixed	CM	CCM MM	√	SO-20N
FAN6921	Combo QR	Variable	VM	BCM	√	SO-16
NCP1937	Combo QR	Variable	VM	BCM	√	
NCP1618	Boost	Variable Fixed	CM	CCM MM	√	SOIC-9
NCP1632	Interleaved	Variable	VM	BCM	—	SO-20

PFC Controllers from

Part-Number	Structure	Operating Frequency	Control Mode	Operating Mode	HV pin	Package
TEA19162HT	Boost	Variable	VM	BCM	—	SO-8
TEA19162T	Boost	Variable	VM	BCM	—	SO-8
TEA2017AAT	Combo LLC	Variable Fixed	CM	CCM MM	√	SO-16
TEA2016AAT	Combo LLC	Variable Fixed	CM	CCM MM	√	SO-16

- ✓ The two standalone PFCs can be teamed up with LLC controller TEA19161T

PFC Controllers from

Part-Number	Structure	Operating Frequency	Control Mode	Operating Mode	HV pin	Package
ICE2PCS01/G	Boost	Adjustable	CM	CCM	—	DIP/SO-8
ICE3PCS01G	Boost	Adjustable	CM	CCM	—	SO-14
ICE3PCS03G	Boost	Adjustable	CM	CCM	—	SO-8
ICE3PCS05/G	Boost	Adjustable	CM	CCM	—	DIP/SO-8
IRS2505LPBF	Boost	Variable	VM	BCM	—	SOT23-5

✓ ICE3PCS03G and ICE3PCS01G include an internal digital compensation

PFC Controllers from

life.augmented

Part-Number	Structure	Operating Frequency	Control Mode	Operating Mode	HV pin	Package
L6562A	Boost	Variable	VM	BCM	—	DIP/SO-8
L6563S	Boost	Variable	CM	BCM	—	SO-14
L6564	Boost	Variable	CM	BCM	—	SSOP-10
L6564H	Boost	Variable	CM	BCM	√	SO-14
L4984D	Boost	Nearly Fixed	CM	FOT	—	SSOP10
STCMB1	Combo LLC	Variable Fixed	VM	BCM	√	SO-20W

Conclusion

- ❑ Nonlinear loads force the unnecessary circulation of reactive power
- ❖ Reactive power flows in the grid and heats up distribution wires
- ❑ Mains rectification brings a poor power factor and distorts the current
- ✓ Power factor correction forces the absorption of a sinusoidal current
- ✓ It reduces the circulating reactive power and reduces the rms current
- ❑ The boost converter is a popular structure and can operate in:
 - ✓ Borderline conduction mode up to 200-300 W
 - ✓ Continuous conduction mode for high output levels beyond 1 kW
 - ✓ Multi-mode combine best of both worlds for optimized efficiency
- ❑ The totem-pole PFC becomes popular owing to wide-bandgap components
- ❑ A PFC is a closed-loop system: pay attention to the stability